

Reacting Fluids Laboratory  
Department of Chemical Engineering  
Louisiana State University  
Baton Rouge, Louisiana

STATUS REPORT

on

NON-EQUILIBRIUM FLOW AND THE KINETICS  
OF CHEMICAL REACTIONS IN THE CHAR ZONE

N.A.S.A. Grant NGR 19-001-016

Evaluation of the Energy Transfer  
in the Char Zone During Ablation

by

Ralph W. Pike, Associate Professor  
Principal Investigator  
Gary C. April, Graduate Associate  
Eduardo G. del Valle, Graduate Associate

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## I SUMMARY

In the temperature range from 500°F to 2500°F non-equilibrium flow analysis predicted only a small change in degradation product composition as the gases flow through the char zone. Essentially all of the reaction took place in the temperature range from 2000°F to 2500°F. Comparing non-equilibrium flow with the two limiting cases the energy absorbed in the char zone for frozen flow was one half of that of non-equilibrium flow, and equilibrium flow was two and one half times that of non-equilibrium flow.

Experimental results were obtained simulating the char zone during ablation in the temperature range from 900°F to 1650°F using the Char Zone Thermal Environment Simulation System. The data showed that the flow was essentially frozen, and this was accurately predicted by the non-equilibrium flow analysis. The limiting case of equilibrium flow incorrectly predicted significant changes in degraded product composition in this temperature range.

Details are given concerning the criteria used for selecting the chemical reactions that were important in the char zone, the generalized reaction kinetics analysis, the computer solutions of the equations and the experimental system.

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## II. INTRODUCTION

The primary objective of this research program is to determine accurately the energy absorbed in the char zone of a charring ablator, and how this is affected by the chemical reactions that take place in the char zone. Presently, there are two methods available to describe the limits on the heat transfer in the char zone. These are referred to as the frozen flow and equilibrium flow cases.

The minimum amount of energy that can be absorbed in the char zone can be computed by considering the flow to be frozen. This refers to the situation where the degradation products flowing through the char do not undergo any chemical reactions (the composition is constant). The amount of energy absorbed is given by the change in sensible heat of the gases.

The maximum amount of energy that can be absorbed in the char zone is obtained by considering the chemical species in the flow field to be in thermodynamic equilibrium. This refers to the situation where the degradation products undergo reaction at an infinitely fast rate, and the amount of energy absorbed is computed by considering the species to be in thermodynamic equilibrium. This gives the maximum energy absorbed since the reactions are nearly all endothermic.

The limits on the energy transfer established by these two cases have been previously reported (1, 2). It was found that the amount of energy that could be absorbed was almost an order of magnitude greater for equilibrium flow than for frozen flow for the same front and back surface temperatures on the char. Due to the high mass flux of gases from the plastic decomposition the actual amount of energy that is absorbed lies somewhere between these two limiting cases and is determined by the rates of chemical reaction among the species present.

In this report the necessary equations are developed to compute the energy absorbed in the char zone. These equations are solved for non-equilibrium flow in the char and for the two limiting cases of frozen and equilibrium flow. Comparisons are made between the computed results and experimental data obtained on the Char Zone Thermal Environment Simulator System which is also described. Details are given for the generalized reaction kinetics analysis and the criteria used for solution of the reactions that are important in the char zone. Also included are descriptions, flow diagrams and print-outs of the computer programs used in the computations.

### III. ENERGY AND MOMENTUM TRANSFER IN NON-EQUILIBRIUM FLOW

To compute the energy transferred and the pressure distribution in the char zone, it is necessary to solve the energy equation and momentum equation with appropriate boundary conditions. For steady flow of degradation products in a char zone of constant thickness, the energy equation has the following form:

$$W_g \cdot \bar{C}_p \cdot \epsilon \cdot \frac{dT}{dz} - \frac{d}{dz} \left[ k_e \cdot \frac{dT}{dz} \right] + \sum_{i=1}^{K+1} H_j r_j = 0 \quad (1)$$

The first term represents the convective heat transfer, the second term represents conductive heat transfer and the third term represents the heat absorbed by chemical reactions. The derivation of this equation and a description of the numerical solution is given in Appendix A.

To describe the pressure distribution a modified form of Darcy's equation was used which accounts for inertial effects that are important due to the high mass flux of degradation products. For the steady flow of an ideal gas in the char with varying mass flux, the following integral equation was obtained to predict the pressure distribution:

$$P = \left\{ P_L^2 + 2R \left[ \epsilon / \gamma \int_z^L (W_g \mu T / \bar{M}) dz + \beta \int_z^L (W_g^2 T / \bar{M}) dz \right] \right\}^{1/2} \quad (2)$$

The first term on the right hand side is the pressure on the high temperature surface of the char, the second and third terms represents the pressure loss due to viscous and inertial effects respectively.

The energy absorbed in the char zone is equal to the difference between the heat flux at the high temperature surface and the heat flux at the low temperature surface. As also shown in Appendix A the energy absorbed

for non-equilibrium flow in the char is given by:

$$q_{cz} = \epsilon \sum_{i=1}^K \int_{T_o}^{T_L} w_g x_j C_p j dT + \sum_{j=1}^{K+1} \int_{T_o}^{T_L} \frac{dN_i}{dT} \cdot M_j \cdot H_j dT \quad (3)$$

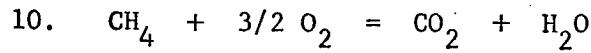
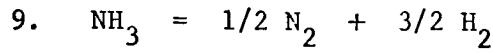
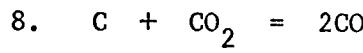
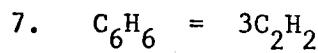
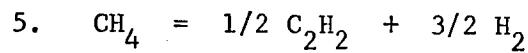
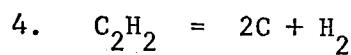
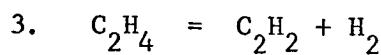
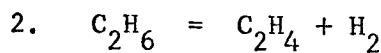
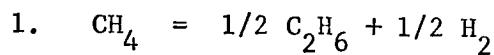
The first term on the right hand side represents the heat absorbed due to the change in enthalpy of the gases and the second term represents the heat absorbed by chemical reactions.

Equations (1), (2) and (3) were solved numerically using programs written in FORTRAN IV on an IBM 7040 computer. This is described in detail in Appendix C where flow diagrams of the sub-programs are given with a print-out of the programs. A subsequent section (Generalized Reaction Kinetics Analysis) discusses the method used to compute the reaction rates of the simultaneous chemical reactions as they occur in the char zone.

However before the calculations can be performed two additional pieces of information must be known. These are the specific chemical reactions that occur in the char with their associated kinetic constants and the initial composition of the degradation products when they enter the char zone. The ten specific chemical reactions that are thought to occur in the char zone are listed in Table 1, and the method of arriving at these reactions is discussed in the following section entitled "Criteria for Reactions Selection." Also discussed in this section are the methods for establishing the initial compositions which were based on the compositions predicted by thermodynamic equilibrium calculations and pyrolysis gas chromatography experiments.

In Figure 1 a comparison is shown of the temperature distribution for non-equilibrium, equilibrium and frozen flow from the solution of the equations of change (continuity, momentum and energy) for a surface temperature

TABLE 1

IMPORTANT CHEMICAL REACTIONS IN THE CHAR ZONE IN THE TEMPERATURE  
RANGE FROM 500 TO 2500°F

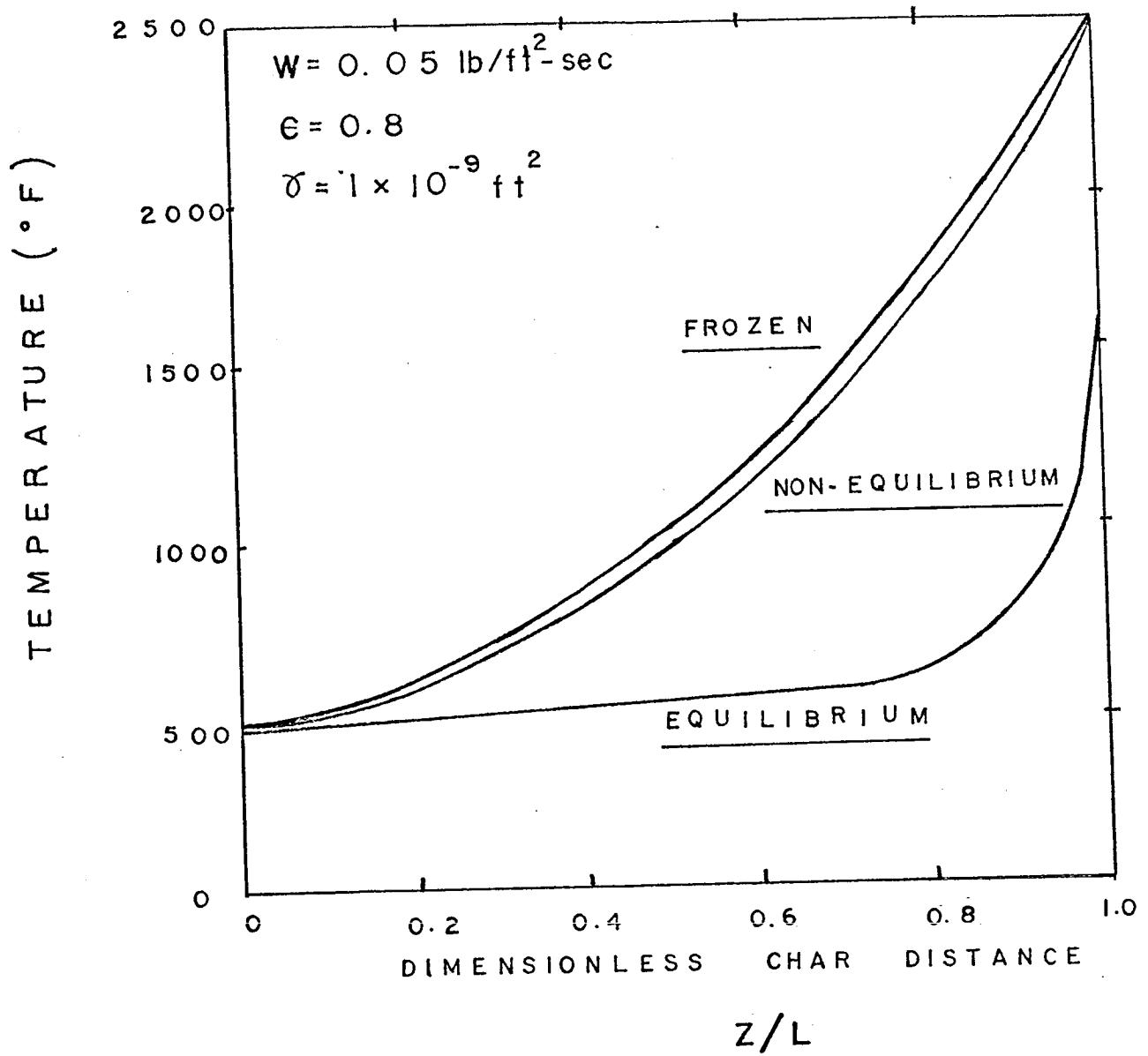


Figure 1. Comparison of the Temperature Distributions for Non-Equilibrium, Equilibrium and Frozen Flow in the Char Zone with a 2500°F Surface Temperature.

of 2500°F. As shown the temperature distribution for non-equilibrium flow is only slightly less than that for frozen flow. However the temperature distribution for equilibrium flow is significantly different than that for frozen and non-equilibrium flow. The effect of small changes in composition due to chemical reactions cause the temperature profile for non-equilibrium flow to only be slightly different than that for frozen flow. However, the temperature profile for equilibrium flow is significantly different than that for non-equilibrium flow, and this is a result of the energy absorbed due to the significant changes in composition determined by thermodynamic equilibrium.

Although the temperature profile is essentially the same there is a significant difference between the heat flux at the high temperature surface for non-equilibrium and frozen flow as seen in Table 2. This is mainly a result of the decomposition of  $\text{CH}_4$  by reactions 1, 5 and 6 and the formation of CO by reaction 8. This is seen in Table 2 by the change in degradation product composition from 500°F to 2500°F. The energy absorbed considering the flow in thermodynamic equilibrium is much larger than that for non-equilibrium flow, and the reason is the large changes in composition as shown in Table 2. Thus if some means could be devised to increase the rate of reactions, there is the potential for a sizeable increase in amount of energy that could be absorbed. This would mean a reduction in heat shield weight.

Given in Table 2 are the pressure drop through the char calculated using equation (2) for non-equilibrium, equilibrium and frozen flow. As would be expected the pressure drop predicted by assuming the flow to be in equilibrium is less than that for either frozen or non-equilibrium flow since the viscosity is an increasing function of temperature. As would

Table 2 - Comparison of the High Temperature Surface Heat Flux, Composition of Degradation Products and Pressure Drop for Frozen, Equilibrium, and Non-Equilibrium Flow

Mass Flux - 0.05 lb per ft<sup>2</sup> - sec

Char Characteristics: Porosity - 0.8  
Permeability -  $1 \times 10^{-9}$  ft<sup>2</sup>

DEGRADATION PRODUCT COMPOSITION (Mole Percent)

<u>Component</u>	<u>Entering the Char</u>	<u>Leaving the Front Surface at 2500° F</u>	
	<u>At 500° F</u>	<u>Non-Equilibrium Flow</u>	<u>Equilibrium Flow</u>
CH <sub>4</sub>	55.47	54.50	0.10
H <sub>2</sub> O	32.48	33.20	0.01
N <sub>2</sub>	8.06	8.00	4.21
CO <sub>2</sub>	1.52	0.02	Trace
H <sub>2</sub>	1.45	1.44	77.03
NH <sub>3</sub>	0.02	0.01	Trace
CO	Trace	1.71	18.65

<u>Model</u>	<u>Heat Flux at Surface</u> <u>(BTU/ft<sup>2</sup>-sec)</u>	<u>Pressure Drop</u> <u>(lb/ft<sup>2</sup>)</u>
Frozen Flow	52.22	12.97
Non-Equilibrium Flow	107.64	12.45
Equilibrium	271.25	9.75

be expected the pressure drop for non-equilibrium and frozen flow is essentially the same.

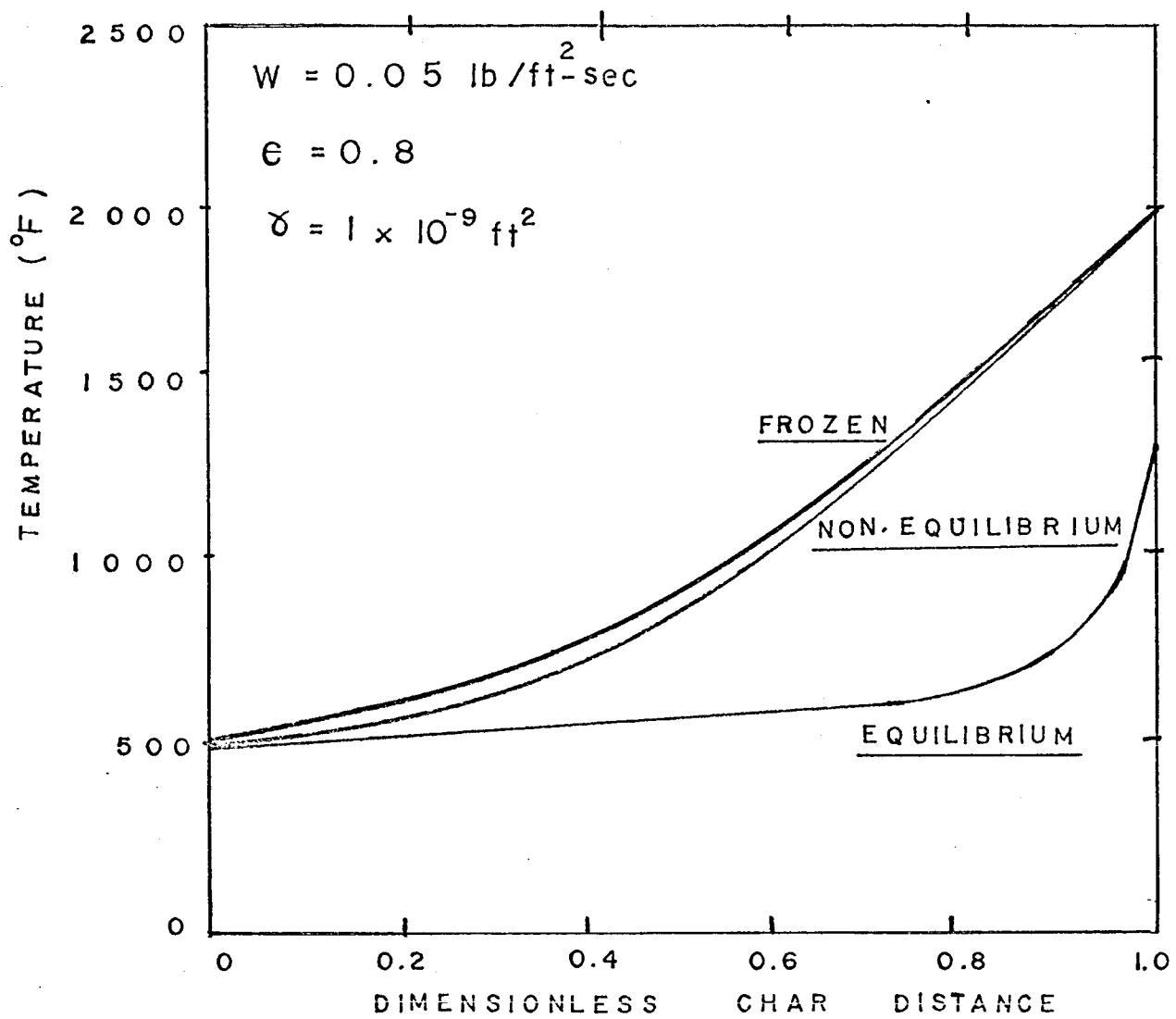
In Figure 2 similar results to that of Figure 1 and Table 2 are shown except for a front surface temperature of 2000°F. As would be expected the temperature profiles are similar to that of Figure 1. However, on comparing the surface heat flux it is seen that there is only a slight difference between that for frozen and non-equilibrium flow. Consequently the major energy absorption occurs in the temperature range from 2000°F to 2500°F. This would be expected since the rate of reaction increases exponentially with temperature. Thus it would also be expected that for cases with higher char temperatures the heat absorbed by chemical reactions would be much more significant. Currently work is underway to extend these analyses to higher surface temperatures.

#### IV. EXPERIMENTAL SIMULATION OF THE CHAR ZONE DURING ABLATION

##### A. Char Zone Thermal Environment Simulator

Experiments are being conducted to establish the accuracy of the non-equilibrium flow model with an experimental system that simulates the char zone during ablation. A schematic diagram of the Char Zone Thermal Environment Simulator is shown in Figure 3.

In this simulator actual chars formed in the large arc jets at the Langley Research Center are mounted in a char holder as shown. The holder is constructed of concentric tubes so gases of compositions that are typical of the degradation products can flow through the char as they would have on leaving the decomposition zone. Chars are removed from 3" diameter arc jet samples, and saureisen cement is poured around the sides of the char inside a mold. This mounts the char with front and back surface



MODEL	SURFACE HEAT FLUX BTU / ft <sup>2</sup> - sec	PRESSURE DROP LB / ft <sup>2</sup>	MIDPOINT TEMPERATURE °F
FROZEN	44.67	15.3	948.7
NON-EQUILIBRIUM (10 REACTIONS)	45.17	15.1	890.6
EQUILIBRIUM	180.83	9.22	537.6

Figure 2. Comparison of the Solutions of the Energy and Momentum Equations for Non-Equilibrium, Equilibrium and Frozen Flow in the Char Zone with a 2000°F Surface Temperature.

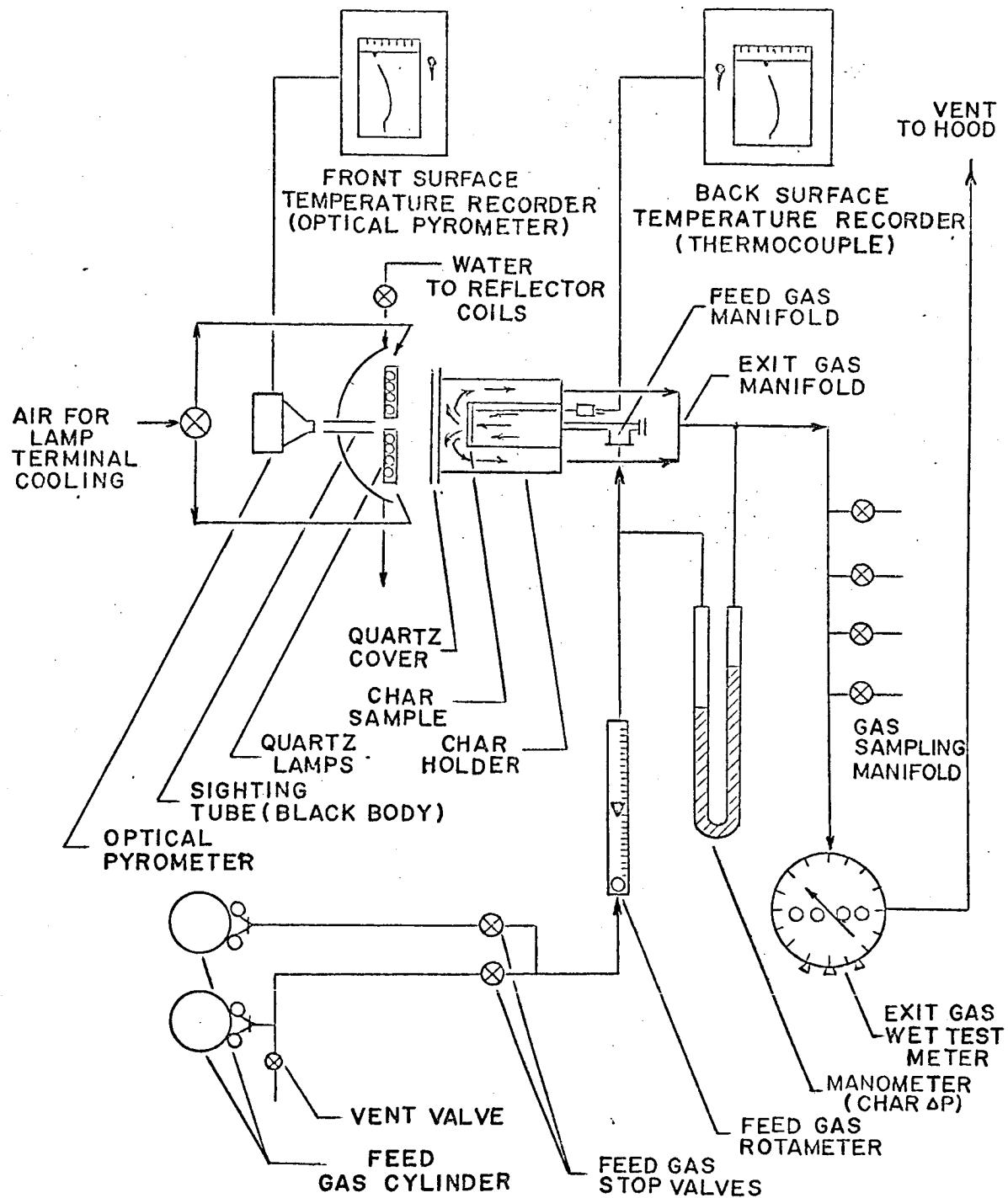


FIGURE 3

CHAR ZONE THERMAL ENVIRONMENT SIMULATOR

exposed in a uniform inert ceramic casing which is mounted in the char holder.

To have a temperature profile comparable to that on re-entry a bank of 15 G. E. 1000 T3 quartz lamps are used to heat the char surface. The bank is located about 1-1/2' from the char surface, is surrounded by a reflector, and has a total output of about 15 KW.

A total radiation pyrometer (Leeds and Northrup, Narrow Angle Rayotube) is focused on the front surface of the char through the bank of lamps to give an accurate measure of the front surface temperature. This is recorded on a strip chart recorder. This accuracy ( $\pm 20^{\circ}\text{F}$  at  $2000^{\circ}\text{F}$ ) was established by comparing the temperature measured by the total radiation pyrometer with that of a calibrated optical pyrometer. Also it was established that the pyrometer was not being affected by sighting through the quartz lamps. This was accomplished by operating the lamps without the char holder in place, and with the lamp on the pyrometer did not register an increase in temperature. The usual corrections to the measured temperature due to the reflected radiation from the lamps were made. This correction was less than  $25^{\circ}\text{F}$  at a char surface temperature of  $1650^{\circ}\text{F}$ .

The back surface temperature was measured with a shielded iron-constantan thermocouple and recorded on a strip chart recorder. The thermocouple made firm contact with the char surface to insure an accurate surface temperature measurement. The thermocouple responded very rapidly when the bank of heating lamps was turned on indicating that good contact was being made between the char surface and the thermocouple tip.

A blend of gases simulating the composition of the degradation products was made in a high pressure cylinder. The composition of feed blend number one is reported in Table 3. The gas is passed through a regulator

and is metered by a calibrated rotameter to the char holder. Having passed through the char the gases flow through a sample manifold where periodic samples are taken for gas chromatographic analysis and then through a wet test meter where volume (flow rate) is measured.

The composition of the feed and products are analyzed on a Packard Instrument Corporation gas chromatograph with a thermal conductivity detector. Hydrocarbons and  $\text{CO}_2$  are determined on a 12 ft. column filled with Porapak S packing with helium as a carrier gas. Nitrogen, oxygen and carbon monoxide are determined on a 6 ft. column packed with 5A molecular sieve with helium as a carrier gas. Hydrogen is determined on this column using argon as a carrier gas.

The pressure drop across the char is measured with a U-tube manometer using water as the manometer fluid. The taps of the manometer are located on the entrance and exit gas lines. The actual pressure drop across the char is determined by subtracting from the total pressure drop, the pressure drop measured without the char in place. The pressure drop without the char in place for the range of flow rates employed in the test was less than 0.5 inch of water.

The operating procedure consisted of a start-up phase, a steady state phase, and a shut-down phase. In the start-up phase cooling water and air flow rates are adjusted, recorders are started, helium flow through the char is set and then power is applied to the bank of lamps. The temperature of the system rises to a steady-state value, and now in the steady-state phase at these conditions a set of data are collected which represents frozen flow in the char. Then the flow is switched to a feed of a composition typical of the degradation products. When temperature transients have damped (about 3-5 minutes), product samples are taken at 5 minute intervals for a run time of more than 20 minutes. Operating conditions are then changed to obtain another set of

data or the system is shut down.

To shut-down the operation of the system, the flow through the char is changed to helium and then the power to the lamps is turned off. The system is allowed to cool to near room temperature and all of the flows are turned off.

### B. Experimental Results

In Table 3 a comparison is given between typical experimental results (0.005 lb per  $\text{ft}^2\text{-sec}$  mass flux, 1650°F front surface temperature, 900°F back surface temperature) and the models for non-equilibrium and equilibrium flow. The inlet composition is the concentration of the stream entering the char at 900°F and the outlet composition is the concentration leaving the front surface of the char at 1650°F. The experimentally measured values are shown in Table 3 along with the values that are computed by the model of non-equilibrium flow and equilibrium flow. As shown the amount of chemical reactions that actually took place was only slight and this is accurately predicted by non-equilibrium flow. The computed values of the composition agree within experimental error with the experimental values. For this temperature range the flow is essentially frozen (no chemical reaction).

For comparison the exit composition computed for equilibrium flow is also given in Table 3. If the gases were actually in thermodynamic equilibrium flowing through the char, there would have been a significant heat absorption due to reaction. In fact nearly all of the methane is decomposed and essentially all of the carbon dioxide is converted. Thus this would be an extremely poor characterization of the flow to consider it to be in thermodynamic equilibrium in this temperature range and unrealistically high surface heat flux values would be computed as shown in Figure 4.

Table 3. Comparison Between a Typical Set of Experimental Results  
(Experimental Test 9) and Non Equilibrium Flow Computations

Operating Conditions: Mass Flux - 0.005 lb/ft<sup>2</sup> sec

Surface Temperatures: Front - 1650°F  
Back - 900°F

Char - Specimen No. 52\*, Thickness - 0.25 inch.

Degradation Product Compositions (mole per cent)

<u>Component</u>	<u>Inlet Composition</u>	<u>Outlet Composition</u>		
		<u>Experimentally Measured</u>	<u>Computed Non-Equil. Flow</u>	<u>Computed Equil. Flow</u>
CH <sub>4</sub>	44.61	44.68	43.40	1.52
H <sub>2</sub>	35.81	35.79	35.01	81.91
N <sub>2</sub>	11.13	11.12	12.68	7.59
CO <sub>2</sub>	4.75	4.70	5.21	0.02
CO	3.71	3.80	3.70	8.65
H <sub>2</sub> O	0	0	0	0.31
Total	100.00	100.00	100.00	100.00

Pressure Gradient Across Char

Experimentally Measured - 2.1 psf

Computed by Non-Equilibrium Flow - 2.3 psf

\*Low density phenolic-nylon tested in Langley Research Center arc jet using a 4 in. dia. nozzle with a 3% O<sub>2</sub> - 97% stream having a 2000 Btu/# stream enthalpy at a heating rate of 100 Btu/ft<sup>2</sup> sec. and at a test time of 100 sec.

The pressure drop computed by equation (2) is compared with the experimentally measured pressure drop in Table 3. As can be seen there is excellent agreement between the experimental and computed values.

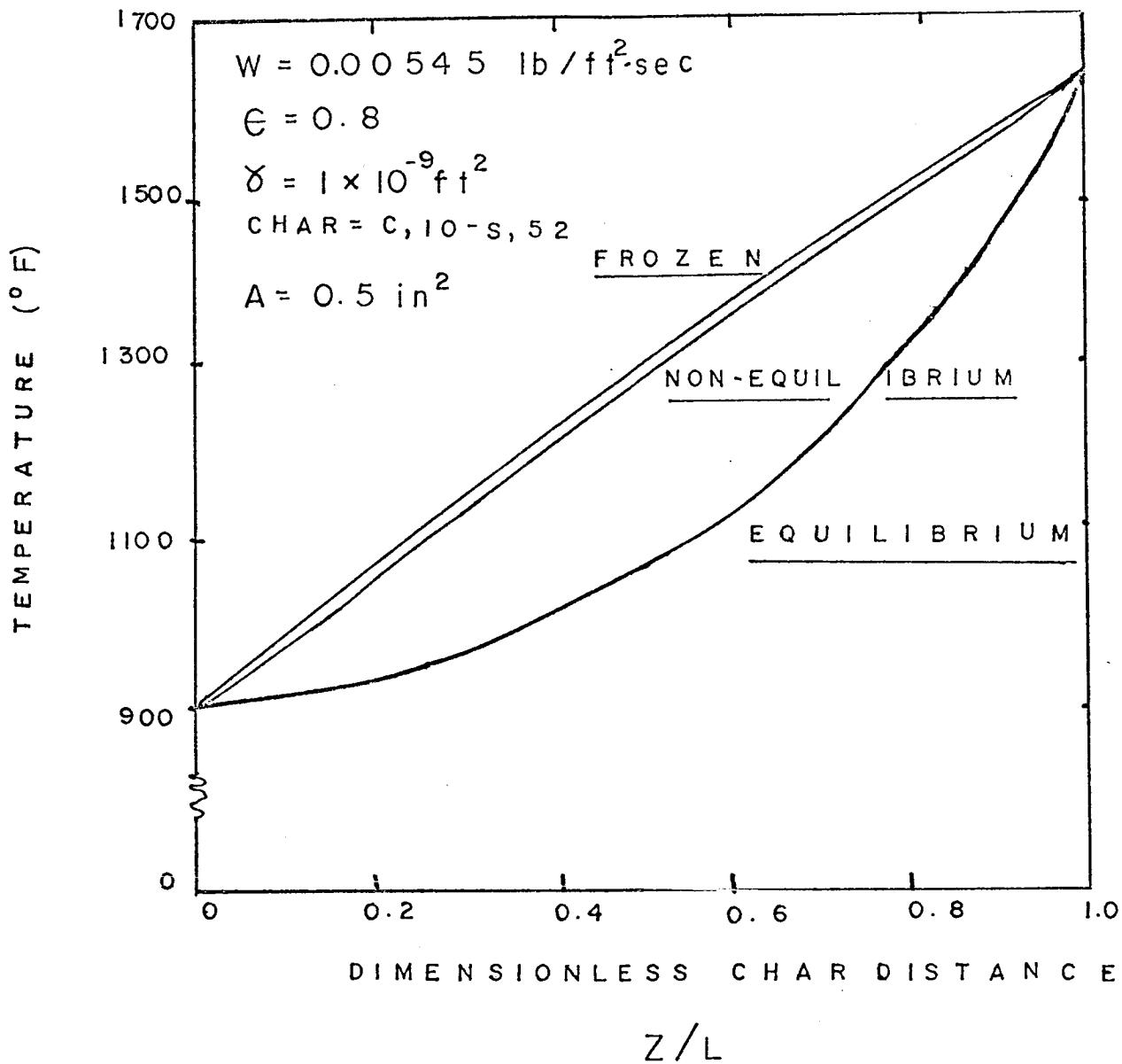
As a means for further comparison the temperature profile for each of the three flow models is presented in Figure 4. The non-equilibrium flow temperature profile lies very near the profile for frozen flow while the equilibrium flow deviates significantly as would be expected. The energy absorbed due to chemical reactions is shown by the increase of 0.85 Btu/ $\text{ft}^2\text{-sec}$  in the surface heat flux over that of frozen flow. However, the heat flux predicted for equilibrium flow is over 6 times that for non-equilibrium flow. This high and notrealistic surface heat flux is due to the large change in composition.

In conclusion it can be stated that in the temperature range of the experiments only a small change in composition occurs due to chemical reactions as the gas flows through the char. This is due to the short residence time of the gas in the char as a result of the high mass flux through the char. The flow is essentially frozen. If the chemical species are assumed to be in thermodynamic equilibrium flowing through the char, there would be over a six fold error in computing the surface heat flux, i.e. the energy absorbed in the char zone.

#### V. GENERALIZED REACTION KINETICS ANALYSIS

The purpose of this section is to present the equations that permit the calculation of the reaction rates for an arbitrary number of simultaneous chemical reactions involving an arbitrary number of chemical species. This will be illustrated with the reactions given in Table 1.

A chemical reaction can be written in general as:



MODEL	SURFACE HEAT FLUX <u>BTU/FT<sup>2</sup> SEC</u>	PRESSURE DROP <u>LB/FT<sup>2</sup></u>	MIDPOINT TEMPERATURE, $^{\circ}$ F
FROZEN	2.73	2.27	1276.5
NON-EQUILIBRIUM	3.58	2.25	1274.7
EQUILIBRIUM	23.50	1.76	1049.3

Figure 4. Comparison of Momentum and Energy Transfer Computed For Experimental Test 9.



For this  $i$  th chemical reaction, the  $r_{ij}$  and  $p_{ij}$  represent the stoichiometric coefficients of the reactants and products respectively for species  $A_j$ . The forward and reverse reaction rate constants are  $k_{fi}$  and  $k_{ri}$ . There are a total of  $K$  chemical species.

For the rate of reaction of the  $j$ th species,  $R_j$ , this is given by the following equation for  $n$  chemical reactions:

$$R_j = \sum_{i=1}^n (p_{ij} - r_{ij}) \left[ k_{fi} \prod_{j=1}^K c_j^{r_{ij}} - k_{ri} \prod_{j=1}^K c_j^{p_{ij}} \right] \quad (5)$$

where  $c_j$  is the concentration of component  $j$  in appropriate units.

This equation has the powers on the composition terms the same as the stoichiometric coefficients. However, it is not necessary to do this. If this is not the case for some of the reactions being used, it is only necessary to include two additional matrices besides  $r_{ij}$  and  $p_{ij}$  in the computer implementation.

To illustrate the use of equations (4) and (5) the matrix form of the reactions listed in Table 1 are shown in Table 4. This is equation (4) for 10 reactions and 13 chemical species.

To illustrate the use of equation (5), the rate of reaction of methane (component 2) is given by the following:

$$r_2 = \sum_{i=1}^{10} (p_{i2} - r_{i2}) \left[ k_{fi} \prod_{j=1}^{13} c_j^{r_{ij}} - k_{ri} \prod_{j=1}^{13} c_j^{p_{ij}} \right] \quad (6)$$

or expanding

Table 4. Matrix Formulation of the Chemical Reactions Given in Table 1

$$\begin{aligned}
 r_2 = & (0 - 1) \left\{ k_{f1} c_2 - k_{r1} c_1^{\frac{1}{2}} c_3^{\frac{1}{2}} \right\} + \\
 & (0 - 1) \left\{ k_{f5} c_2 - k_{r5} c_1^{3/2} c_5 \right\} + \\
 & (0 - 1) \left\{ k_{f6} c_2 - k_{r6} c_1^2 c_6 \right\} + \\
 & (0 - 1) \left\{ k_{f10} c_2 c_{12}^{\frac{1}{2}} - k_{r10} c_8 c_{13} \right\} \quad (7)
 \end{aligned}$$

The above equation contains six other terms in the expanded form, but these are not included since the coefficients were zero. Of course this equation is not exactly correct since the powers on the compositions are different in some cases for the actual rate expressions. For example, the carbon-carbon dioxide reaction involves the surface area of carbon, and not a "concentration" of carbon. To take the surface area of the char into account the reaction rate constant can be modified, and the exponent on the carbon "concentration" can be set equal to zero.

Equation (5) has been incorporated into the main program which generates the solution to the energy equation using a fourth order Runge-Kutta Method (1). With this it is possible to predict the energy absorbed in the char zone for non-equilibrium flow. Some of these results have been presented in a preceding section along with a comparison of experimental results obtained by flowing typical compositions of degradation products through actual chars. Additional experimental results will be presented in a subsequent report.

#### VI. CRITERIA FOR REACTION SELECTION

In a previous report (3) the literature was surveyed for the kinetics of chemical reactions that could possibly occur in the char zone during ablation. At that time a number of reactions and species were located,

and since then additional information has become available. These results have been up-dated and will be presented in a forthcoming report. However, it can be shown that not all of these possible reactions are important in the temperature range of interest. To determine the chemical reactions that would occur with a significant conversion in the char, two procedures were used. One procedure consists of computing the conversion for one reaction of an equal molal mixture of reactants flowing isothermally through the char. The other procedure consist of estimating the species and the composition that enter the char zone from thermal-gravimetric analysis and pyrolysis gas chromatographic analysis. These two procedures combined determine the important reactions that occur in the char, and these are discussed in the next sections.

#### A Isothermal Flow Analysis

There is a sizeable number of possible chemical reactions that can occur in the char zone as was previously discussed. To attempt to include all of these reactions in the solution of the energy equation to predict the energy absorbed in the char zone for non-equilibrium flow would be very difficult. Consequently it was necessary to devise a screening procedure to eliminate from consideration the reactions that are not important in the temperature range of current interest ( $500^{\circ}\text{F}$  -  $2500^{\circ}\text{F}$ ). The following reasoning was applied.

The rate of reaction increases with temperature. For a particular reaction, if a significant conversion of reactants to products was obtained with the char at a uniform and high temperature, then it could be assumed that there may be a significant conversion when the char is subjected to a temperature gradient (low temperature at  $500^{\circ}\text{F}$  to a high temperature at  $2500^{\circ}\text{F}$ ). Thus these reactions should be considered in any analysis of the char zone.

Conversely if there is essentially no conversion at a high temperature ( $2500^{\circ}\text{F}$ ) for the char at this uniform temperature, there will be no conversion with an increasing temperature gradient in the char. Thus these reactions can be eliminated from consideration. Correspondingly if there is complete conversion within the char at a low temperature, there will be complete conversion for the case of a temperature gradient. Thus this reaction can be eliminated from consideration and only the products are considered to be present.

To determine the important chemical reactions in the temperature range from  $500^{\circ}\text{F}$  to  $2500^{\circ}\text{F}$ , the conversion of an equal molal mixture of the reactants flowing in the char was determined at mass flux rates of 0.01 and 0.05 lb per  $\text{ft}^2\text{-sec}$  for nearly all of the reactions reported in reference (3) and some additional reactions. These results are tabulated in Appendix B for temperatures from  $500^{\circ}\text{F}$  to  $3000^{\circ}\text{F}$  in  $500^{\circ}\text{F}$  intervals for a mass flux of 0.01 lb per  $\text{ft}^2\text{-sec}$ . The lower mass flux rate gave a longer residence time of the species in the char, and consequently a higher conversion. However, in comparing the conversions in general there was only a relatively small decrease in conversion due to the five-fold increase in the mass flux rate. Consequently only the conversions are reported at a mass flux of 0.01 lb per  $\text{ft}^2\text{-sec}$  in Tables B1 through B4.

In Figure 5 the conversion for two reactions are given as a function of temperature. These are the thermal decomposition of pure ethylene and pure acetylene. It can be concluded by examining this figure that there would be no conversion of ethylene in the char for temperatures less than  $1000^{\circ}\text{F}$  and no conversion of acetylene for temperatures less than  $2000^{\circ}\text{F}$ . However the thermal cracking of ethylene would be important for temperatures above  $1000^{\circ}\text{F}$  and for acetylene above  $2000^{\circ}\text{F}$ .

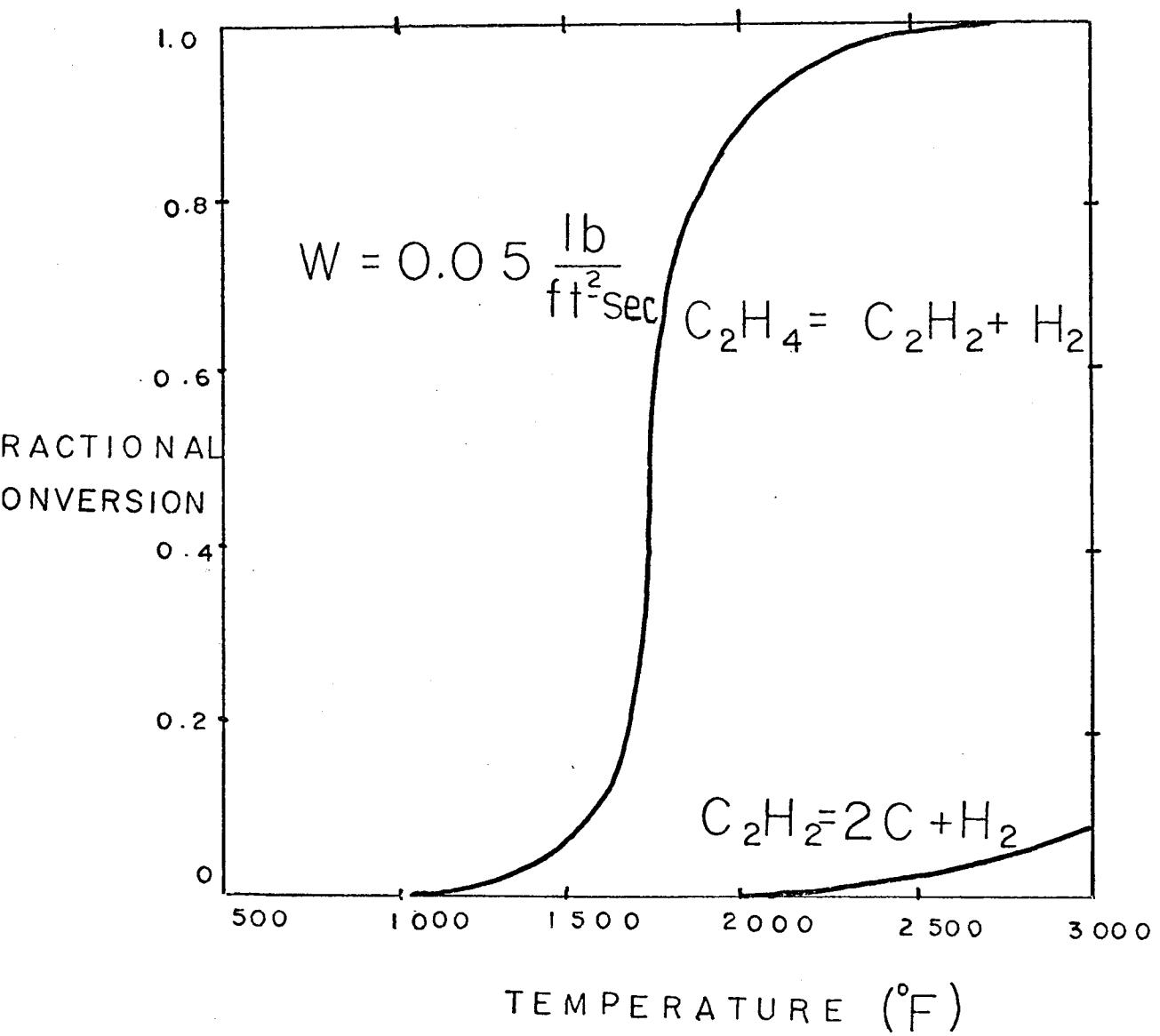
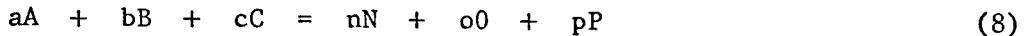


Figure 5. Conversion as a Function of Temperature for the Thermal Decomposition of Pure Ethylene and Pure Acetylene Flowing Isothermally in the Char.

To make the discussion quantitative, the conversion of a reactant is defined as the ratio of the amount consumed by reaction to the amount present initially. To determine the conversion of a chemical reaction of the form:



a material balance is made on component  $j$  flowing through a volume section of the char of area  $A$  and width  $\Delta z$  as shown in Figure 6. If  $N_j$  is the molal flux of component  $j$  at  $z$ , the material balance on component  $j$  for steady flow in the  $z$  direction is:

accumulation of component  $j$  = input of component  $j$  - output of component  $j$

$$0 = N_j M_j A \Big|_z + r_j M_j A \Delta z - N_j M_j A \Big|_{z+\Delta z} \quad (9)$$

where  $r_j$  is the rate of formation of species  $j$  by chemical reaction. Rearranging the above and taking the limit as  $\Delta z$  approaches zero gives:

$$\frac{dN_j}{dz} = r_j \quad (10)$$

The fractional conversion  $X_j$  of component  $j$  is defined as:

$$X_j = (N_{j0} - N_j) / N_{j0} \quad (11)$$

where  $N_{j0}$  is the molal flux of component  $j$  entering the char zone. Differentiating the above with respect to  $z$  gives:

$$N_{j0} \cdot \frac{dX_j}{dz} = - \frac{dN_j}{dz} \quad (12)$$

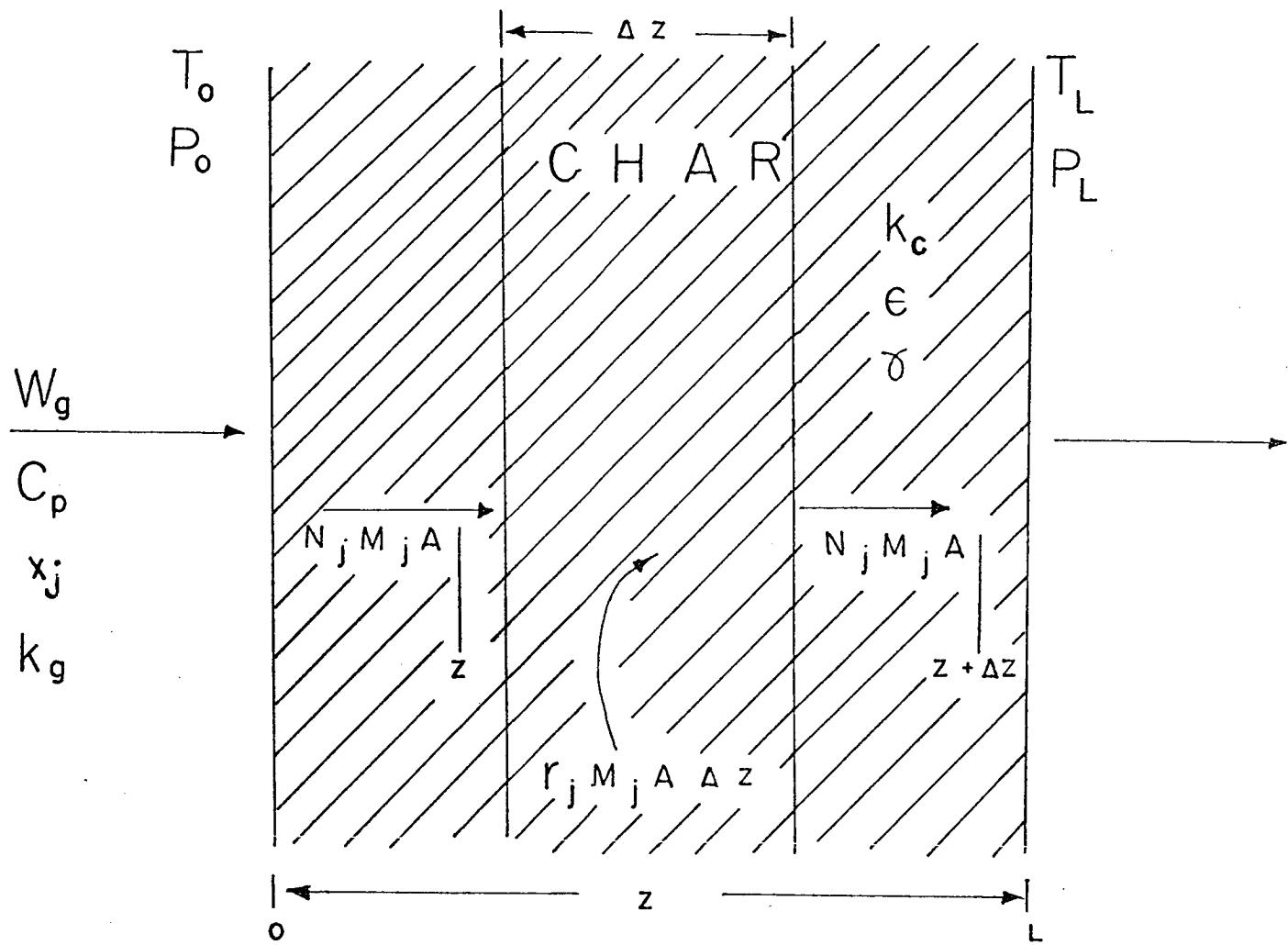


Diagram of the Char Zone

Figure 6

The continuity equation in terms of the volumetric flow rate  $Q$  of gas entering the char is:

$$Q = (N_{j0}/x_{j0}) \bar{M}_o A / \rho \quad (13)$$

Equation (10) using equations (12) and (13) becomes:

$$\frac{\rho x_{j0}}{\bar{M}_o} \cdot \frac{dx_j}{-r_j} = \frac{A}{Q} dz \quad (14)$$

This can be integrated from the front surface of the char where  $x_j$  and  $z$  are zero to the back surface at  $z = L$  where  $x_j = x_{jL}$  and the result is:

$$\frac{\rho x_{j0}}{\bar{M}_o} \int_0^{x_{jL}} \frac{dx_j}{-r_j} = \frac{A \cdot L}{Q} = \frac{V}{Q} = S_t \quad (15)$$

where  $S_t$  is the average residence time or space time, i.e., the average time a molecule stays in the char.

The reaction rate  $r_j$  for component A of equation (8) has the form:

$$r_A = -k_f C_A^a C_B^b C_C^c + k_r C_N^n C_O^o C_P^p \quad (16)$$

and this is needed to integrate equation (15). A trial and error solution of the above integral equation is necessary to determine the final conversion  $x_{jL}$  since the average residence time,  $S_t$ , is known for a given char depth and decomposition products mass flux.

A computer program was written which obtains the solution for equation (15) using equation (16). The final conversion is varied in the solution technique until the calculated value of  $S_t$  corresponds to the known  $S_t$  to

with 0.1%. A Simpson's rule integration is employed to evaluate the integral of equation (15). A flow diagram of the program is given in Figure B1 of Appendix B along with a print-out of the program and a set of typical calculations.

The results of the computations using this program are given in Tables B-1 through B-4. This includes the conversion for each reaction as a function of temperature from 500°F to 3000°F in steps of 500°F. As is seen there are a number of reactions which have a significant conversion in this temperature range. All of these reactions could occur in the char zone if the reactants are among the species formed by the phenolic resin-nylon decomposition, or if the reactants are products from other reactions of the degradation species. A further reduction in the number of reactions can be obtained and is discussed below.

#### B. Estimation of Species Entering the Char Zone

The number of chemical reactions that should be considered for non-equilibrium flow can be reduced further if the composition of the plastic degradation products entering the char from the decomposition zone is known. There are two sources to estimate this initial composition - from thermodynamic equilibrium calculations and from thermal-gravimetric and pyrolysis gas chromatographic analyses. A comparison of the initial compositions from these two methods are shown in Table 5. It can be seen that there is agreement in the order of magnitude of each species present.

The results given for the composition of the degradation products from a 50% (wt) phenolic resin - 50% (wt) nylon mixture was computed by the free energy minimization technique described by del Valle, et.al., (4). Other species were also considered to be present and appdared in concentrations of less than  $10^{-20}$  mole per cent. These were atomic and molecular

Table 5. Composition of Degradation Products from Phenolic Resin, Nylon and a 50% Phenolic Resin - 50% Wt. Nylon Mixture in mole percent

<u>Component</u>	<u>Thermalgravimetric and Pyrolysis Gas Chromatographic Analyses</u>				
	<u>Equilibrium Composition Calculated for the Phenolic-Nylon Mixture (4)</u>	<u>Phenolic Resin Only (5)</u>	<u>Nylon - 6 Only (6) ≠</u>		
	<u>at 500°K</u>	<u>at 800°K</u>	<u>at 500°C</u>	<u>100-1000°C</u>	<u>at 400°C</u>
H <sub>2</sub>	1.45	43.25	15.1	50.1	0
H <sub>2</sub> O	32.47	19.01	34.8	23.4	35.4
N <sub>2</sub>	8.06	6.28	0	0	0
NH <sub>3</sub>	0.02	0.02	0	0	0
HCN	10 <sup>-11</sup>	10 <sup>-5</sup>	0	0	0
CO	10 <sup>-3</sup>	1.85	4.5	5.5	0
CO <sub>2</sub>	1.52	3.42	0.9	1.6	55.8
CH <sub>4</sub>	56.48	26.15	7.8	10.0	0
C <sub>2</sub> H <sub>2</sub>	10 <sup>-20</sup>	10 <sup>-10</sup>	0	0	0
C <sub>2</sub> H <sub>4</sub>	10 <sup>-10</sup>	10 <sup>-5</sup>	0	0	0.4
C <sub>6</sub> H <sub>6</sub>	10 <sup>-20</sup>	10 <sup>-13</sup>	0.2	0.2	5.8
C <sub>7</sub> H <sub>8</sub>	*	*	0.8	0.3	0
C <sub>6</sub> H <sub>5</sub> OH	*	*	28.1	7.1	0
(CH <sub>3</sub> ) <sub>2</sub> C <sub>6</sub> H <sub>3</sub> OH	*	*	7.8	1.8	0
Others	<u>0</u>	<u>0</u>	<u>0</u>	<u>0</u>	<u>2.6</u>
Total	100.0	100.0	100.0	100.0	100.0

\* not considered due to the lack of the necessary free energy data for computations.

# liquid products that were obtained during the pyrolysis were not identified, constituted 95% of the total pyrolysis products.

oxygen and atomic hydrogen. The ratio of moles of solid carbon to total moles of gases was 1.55 at 500°K and 1.35 at 800°K.

Results given in Table 5 for the degradation products from phenolic resin by pyrolysis gas chromatographic analysis were reported by Sykes and Nelson (5). The composition is given at 500°C (773°K) and the average from 100°C to 1000°C for comparison. Also for comparison the composition of the degradation products from the pyrolysis of nylon by thermal gravimetric analysis is given in Table 5 from Madorski (6).

Examining these compositions it is seen that the order of magnitude is the same for the composition of the degradation products obtained from thermodynamic equilibrium calculations and a linear blend of the data from the thermal-gravimetric and pyrolysis gas chromatographic analyses. If these are the compounds that enter the char zone in high concentrations and examining the reactions reported in Tables B1 through B4, it can be concluded that the chemical reactions given in Table 1 are the ten important ones in the temperature range from 500°F to 2500°F.

These reactions were included in the non-equilibrium flow analysis to determine the energy transferred in the char zone. The analysis is currently being extended to cover a higher temperature range where a number of other reactions are important.

Nomenclature

A	cross sectional area of the char zone
c	concentration
$H_j$	enthalpy per unit mass of component j
K	number of species
$k_f$	forward reaction rate constant
$k_r$	reverse reaction rate constant
L	width of char zone
$\bar{M}$	average molecular weight of degradation products
$M_j$	molecular weight of component j
$N_j$	molal flux of component j
n	number of chemical reactions
$p_{ij}$	stoichiometric coefficients of the products
Q	volumetric flow rate
q	heat flux
R	universal gas constant
$r_j$	reaction rate of component j in moles per unit time per unit volume
$r_{ij}$	stoichiometric coefficients of the reactants
$s_t$	average residence time
V	volume of the char
$w_g$	mass flux of gas in the char pores
$x_j$	conversion of component j
$x_j$	mole fraction of component j
z	coordinate axis
$\gamma$	permeability

$\Delta$  forward difference operator  
 $\epsilon$  porosity  
 $\rho$  density  
 $\mu$  viscosity

Subscripts

cz refers to char zone  
i refers to chemical reactions  
j refers to specie  
o refers to initial value  
L refers to final value

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IX. APPENDIX A: DEVELOPMENT OF EQUATIONS OF CHANGE FOR FLOW IN THE CHAR ZONE

A. Energy Equation

Referring to Figure 6, the energy equation for one dimensional flow of gases through a porous medium accompanied by chemical reactions is obtained by simplifying the general energy equation (7), and this gives:

$$w_g \epsilon \bar{C}_p \frac{dT}{dz} = \epsilon \frac{d}{dz} \left[ k_g \frac{dT}{dz} \right] - \epsilon \sum_{i=1}^K H_j r_j \quad (A1)$$

The energy equation for the solid phase is:

$$0 = (1 - \epsilon) \frac{d}{dz} \left[ k_c \frac{dT}{dz} \right] - (1 - \epsilon) H_c r_c \quad (A2)$$

Adding equations (A1) and (A2) and defining:

$$k_e = \epsilon k_g + (1 - \epsilon) k_c \quad (A3)$$

as the effective thermal conductivity of the char, gives the differential equation that describes the energy transfer in the char zone:

$$w_g \epsilon \bar{C}_p \frac{dT}{dz} = \frac{d}{dz} \left[ k_e \frac{dT}{dz} \right] - \sum_{j=1}^{K+1} H_j r_j \quad (A4)$$

For frozen flow in the char zone the above equation reduces to equation (A5):

$$w_g \bar{C}_p \epsilon \frac{dT}{dz} = \frac{d}{dz} \left[ k_e \frac{dT}{dz} \right] \quad (A5)$$

Expanding and rearranging results in a second order, ordinary differential equation which when solved gives the temperature profile in the char.

$$\frac{d^2T}{dz^2} = \frac{dT}{dz} \left[ \frac{W_g \bar{C}_p \epsilon}{k_e} - \left( \frac{dk_e}{dT} \right) \left( \frac{dT}{dz} \right) \left( \frac{1}{k_e} \right) \right] \quad (A6)$$

The energy equation for the equilibrium flow model requires the evaluation of the summation term in equation (A4). Equation (10) for the reaction rate,  $r_j$ , can be written as:

$$r_j = \left( \frac{dN_j}{dT} \right) \cdot \left( \frac{dT}{dz} \right) \quad (A7)$$

Substituting (A7) into (A4) expanding and rearranging gives the energy equation for flow with chemical reaction:

$$\frac{d^2T}{dz^2} = \frac{dT}{dz} \left[ \frac{W_g \epsilon \bar{C}_p}{k_e} - \left( \frac{dk_e}{dT} \right) \left( \frac{dT}{dz} \right) \left( \frac{1}{k_e} \right) + \left( \frac{1}{k_e} \right) \cdot \sum_{j=1}^{K+1} \frac{dN_j}{dT} \cdot M_j \cdot H_j \right] \quad (A8)$$

In equations (A6) and (A8), the surface temperatures are specified defining a two point boundary value problem. Therefore, an iterative procedure to find the correct initial slope that satisfies the boundary conditions was required to define the temperature profile in the char.

### B. Momentum Equation

To obtain the pressure distribution within the char zone the momentum equation for flow in a porous media must be solved. Because of the relatively high gas mass flux values ( $W_g \approx 0.06 \text{ lb}/\text{ft}^2\text{-sec}$ ) inertial as well as viscous effects must be included. The equation with these terms is given below for one dimensional flow in a porous media:

$$-\frac{dp}{dz} = \epsilon \mu u/\gamma + \rho \mu u^2 \quad (A9)$$

where  $\epsilon \mu u / \gamma$  represents the viscous term and  $\beta \rho u^2$  the inertial term (11).

To obtain an equation applicable across a finite char thickness, the continuity equation,  $w_g = \rho u$ ; and the ideal gas law,  $\rho = P \bar{M} / RT$  are combined with equation (A9) to give:

$$-\frac{P dP}{\bar{M}} = \frac{RT}{M} \cdot (\epsilon \mu w_g / \gamma + \beta w_g^2) dz \quad (A10)$$

Integrating this equation from the front surface where the pressure is  $P_L$  to any point  $P$  into the char at  $z$  gives:

$$P = \left\{ P_L^2 + 2R \left[ \frac{\epsilon}{\gamma} \int_{z=z}^{z=L} \frac{w_g \mu T dz}{\bar{M}} + \beta \int_{z=z}^{z=L} \frac{w_g^2 T dz}{\bar{M}} \right] \right\}^{1/2} \quad (A11)$$

Evaluation of  $\gamma$  and  $\beta$  from Experimental Data: In order to solve equation (A11) for the pressure profile within the char zone,  $\gamma$  and  $\beta$ , the permeability and inertial coefficient, must be known. Data on  $\gamma$  and  $\beta$  for char materials are very scarce. However some data were recently obtained by Southern Research Institute (12) and these were used in this work. Their data were analyzed using the integrated form of equation (A10) given below:

$$\frac{\bar{M} \Delta(P^2)}{2W \mu RTL} = \frac{\epsilon}{\gamma} + \beta \left( \frac{w_g}{\mu} \right) \quad (A12)$$

A plot of  $\left[ \frac{\bar{M} \Delta(P^2)}{2W \mu RTL} \right]$  vs  $\left( \frac{w_g}{\mu} \right)$  is a straight line with  $\epsilon/\gamma$  as the y-intercept and  $\beta$ , the slope.

A plot of the experimental data from Southern Research Institute (12) is shown in Figure A1.

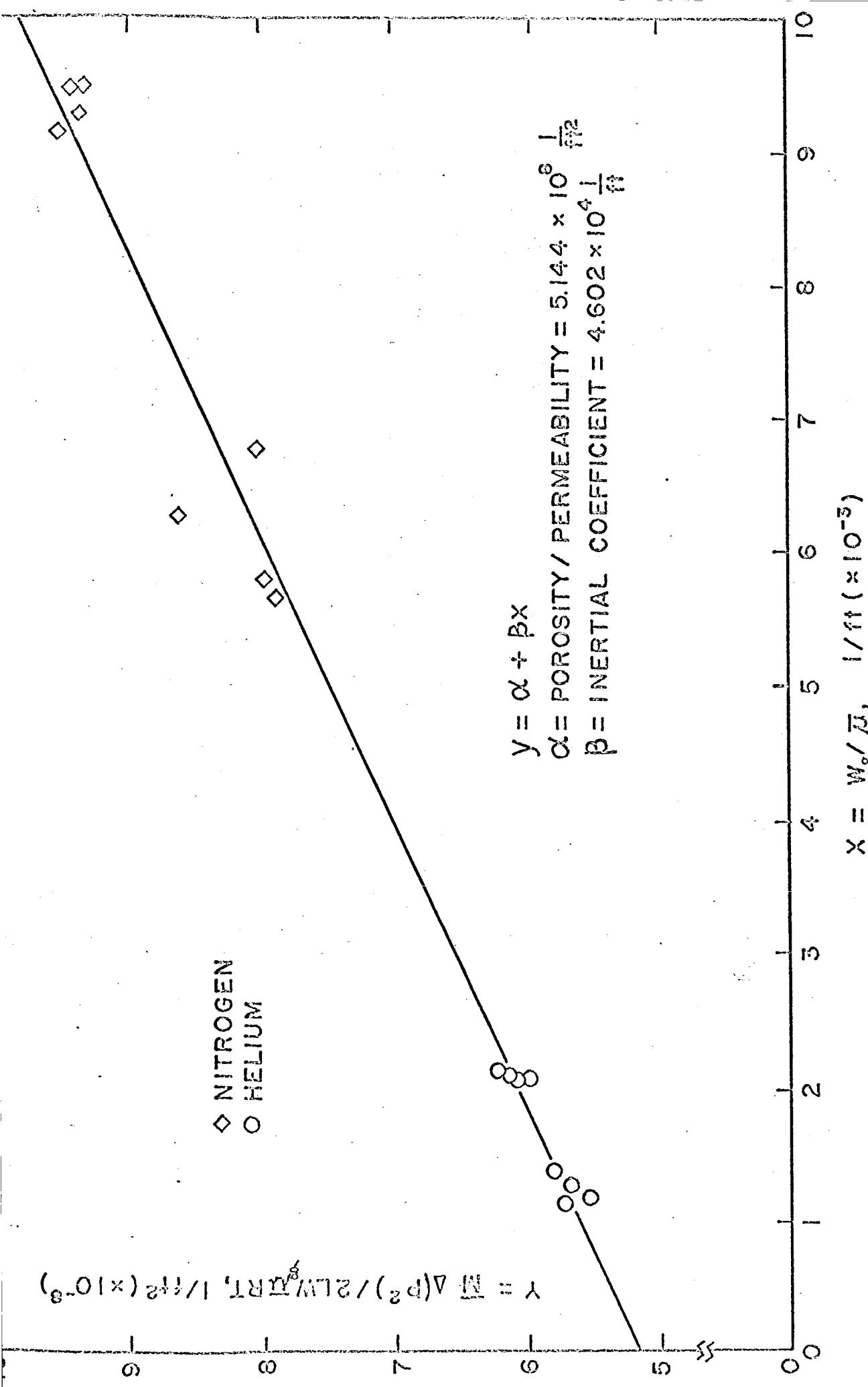


FIGURE A1

CORRELATION OF SOUTHERN RESEARCH INSTITUTE DATA FOR THE PERMEABILITY OF A CHARRED LOW DENSITY PHENOLIC-NYLON RESIN USING A CORNELL-KATZ PLOT

### C. Heat Flux at the Char Surfaces

The heat fluxes at the char surfaces are the heat transfer by conduction to and from the surface and are given by:

$$q_L = k_e \frac{dT}{dz} \Big|_{z=L} \quad (A13)$$

$$q_o = k_e \frac{dT}{dz} \Big|_{z=0} \quad (A14)$$

Frozen Flow: Integrating equation (A5) for frozen flow gives:

$$q_{cz} = (q_L - q_o) = k_e \frac{dT}{dz} \Big|_{z=L} - k_e \frac{dT}{dz} \Big|_{z=0} = \epsilon \int_{T_o}^{T_L} w_g \bar{C}_p dT \quad (A15)$$

where the difference,  $q_{cz} = q_L - q_o$ , is the heat absorbed in the char zone.

Flow with Chemical Reaction: Integrating equation (A4) for flow with chemical reactions gives:

$$q_{cz} = \epsilon \sum_{i=j}^K \int_{T_o}^{T_L} w_g (C_p)_j x_j dT + \sum_{i=1}^{K+1} \int_{T_o}^{T_L} \frac{dN_i}{dT} M_j H_j dT \quad (A16)$$

where  $q_{cz}$  is the heat absorbed by a reacting gas mixture of K components.

### D. Physical Properties

In order to solve equations (1) and (2) the values of the physical properties as functions of temperature are needed. For the heat capacity of each component the usual polynomial form is employed as shown below where the values of the coefficients are obtained from Hougen *et.al.* (8)

and McBride (9).

$$c_{p_i} = a + bT + cT^2 + dT^3 + eT^4 \quad (A17)$$

The mean heat capacity of the gas mixture is calculated using a molal weighted average as shown below:

$$\bar{c}_p = \sum_{i=1}^K (c_{p_i}) y_i \quad (A18)$$

The overall thermal conductivity as a function of the gas conductivity, the char conductivity and the porosity is given by equation (A3).

$$k_e = (\bar{k}_g) (\epsilon) + (k_c) (1 - \epsilon)$$

In this study, experimental data reported for the char conductivity (10) were taken to be equal to the overall thermal conductivity. The reason is that the thermal conductivity measurements were made for char materials containing an inert gas in the pores (10). The equation for the char conductivity was obtained by a least square fit of the data reported for an inert gas within the pores of the char (10).

## XI. APPENDIX B - ISOTHERMAL FLOW ANALYSIS

In this appendix the results of the computations of the conversion as a function of temperature are given for a number of chemical reactions. This is part of the information that was required to select the important reactions that occurred in the char zone in the temperature range from 500°F to 2500°F.

In Table B-1 the conversion of a number of hydrocarbon pyrolysis reactions are given in 500°F intervals from 500°F to 3000°F for a mass flux of 0.01 lb per ft<sup>2</sup> sec. Similar results are given in Table B-2 for a number of oxygen and hydrogen reactions, in Table B-3 for nitrogen and ammonia reactions, and in Table B-4 for carbon, hydrocarbon and oxygen reactions. In Figure B-1 a flow diagram of the program is given that outlines the method of computing the conversion as discussed in the previous section of this report. Following the flow diagram a print-out of the computer program is given in Table B-5 along with a print-out of typical results.

The kinetic constants employed in the calculations were mainly obtained from a literature survey (3). In the comment column of Tables B-1, B-2, B-3, and B-4 the reference is given for the source of the kinetic data. The information given in these four tables should not be considered to be complete as additional data is being found almost every day. A future report will up-date this information and give a comparison of all of the kinetic data found in the literature.

Table B-1 Conversion of Pyrolysis Reactions in Percent for a Mass Flux of 0.01 lb per ft<sup>2</sup>-sec

Equation	Temperature					Comment
	500°F	1000°F	1500°F	2000°F	2500°F	
$\text{CH}_4 \rightarrow 1/2 \text{C}_2\text{H}_6 + 1/2 \text{H}_2$	0	0	0	0	20.3	100 (3)
$\text{CH}_4 \rightarrow \text{C} + 2 \text{H}_2$	0	0	0	2.6	6.6	12.4 (13)
$\text{CH}_4 \rightarrow 1/2 \text{C}_2\text{H}_2 + 1/2 \text{H}_2$	0	0	0	0	4.2	7.4 (3)
$\text{C}_2\text{H}_6 \rightarrow (\text{H}_2, \text{CH}_4, \text{C}_2\text{H}_4, \text{C})$	0	0	15.8	100	100	100 (3)
$\text{C}_2\text{H}_4 \rightarrow (\text{C}_2\text{H}_2, \text{C}_2\text{H}_6, \text{CH}_4, \text{H}_2)$	0	0	8.9	87.9	100	100 (3)
$\text{C}_2\text{H}_2 \rightarrow (\text{C}_1\text{H}_2, \text{TrC}_4\text{H}_2 > 900^\circ\text{k})$	0	0	0	0	1.8	6.7 (3), (14)
$\text{C}_3\text{H}_8 \rightarrow (\text{C}_3\text{H}_6, \text{C}_3\text{H}_4, \text{CH}_4, \text{H}_2)$	0	0	31.1	100	100	100 (3)
$\text{C}_3\text{H}_6 \rightarrow (\text{H}_2, \text{CH}_4, \text{C}_2\text{H}_4, \text{others})$	0	0	2.7	100	100	100 (3)
$\text{C}_3\text{H}_6 + \text{H}_2 \rightarrow \text{CH}_4 + \text{C}_2\text{H}_4 (\text{trC}_3\text{H}_8, \text{C}_2\text{H}_8)$	0	0	0	1.0	15.2	60.9 (3)
Cyclobutane $\rightarrow 2\text{C}_2\text{H}_4$	0	1.2	100	100	100	100 (3)
Methylcyclobutane $\rightarrow \text{C}_2\text{H}_4 + \text{C}_3\text{H}_8$	0	1.1	100	100	100	100 (3)
t-butanol $\rightarrow$ isobutene + $\text{H}_2\text{O}$	0	0	29.0	100	100	100 (3)
Cyclopentene $\rightarrow$ cyclopentadiene + $\text{H}_2$	0	0	70.1	100	100	100 (3)
n-C <sub>4</sub> H <sub>10</sub> $\rightarrow \text{CH}_4 + \text{C}_3\text{H}_6$	0	1.6	100	100	100	100 (3)
Isobutene $\rightarrow$ products	0	0	1.4	97.3	100	100 (3)
C <sub>6</sub> H <sub>6</sub> $\rightarrow 3 \text{C}_2\text{H}_2$	0	0	0	35.7	99.3	100 (3)
C <sub>6</sub> H <sub>6</sub> $\rightarrow 1/2 \text{C}_{12}\text{H}_{10} + 1/2 \text{H}_2$	0	0	54.2	97.0	99.5	99.8 (3)
CH <sub>3</sub> CHO $\rightarrow \text{CH}_4 + \text{CO}$	0	0	0	0	7.4	90.5 (3)

Table B-1 Continued

Equation	500°F	1000°F	1500°F	2000°F	2500°F	3000°F	Comment
$\text{CH}_2\text{O} \rightarrow \text{H}_2 + \text{CO}$	0	0	0	8.1	59.3	98.6	(3)
$\text{CH}_4 + \text{H} \rightarrow \text{H}_2 + \text{CH}_3$	100	100	100	100	100	100	(3)
$\text{CH}_2\text{N}_2 \rightarrow \text{CH}_2 + \text{N}_2$	0	100	100	100	100	100	(3)
$\text{C}_2\text{H}_6 + \text{H} \rightarrow \text{C}_2\text{H}_5 + \text{H}_2$	100	100	100	100	100	100	(3)
$\text{C}_2\text{H}_4 + \text{H}_2 \rightarrow \text{C}_2\text{H}_6$	0	0	0	1.2	11.6	44.7	(3)

Table B-2 Conversion of Hydrogen, Oxygen and Hydrogen - Oxygen Reactions in Percent for a Mass Flux of

0.01 lb per ft<sup>2</sup> sec.

Equation	500°F	1000°F	1500°F	2000°F	2500°F	3000°F	Comment
$H_2 + M \rightleftharpoons 2H + M$	0	0	0	---	---	---	(3)
$O_2 + M \rightleftharpoons 2O + M$	0	0	0	0	---	---	(3)
$2O_2 \rightleftharpoons O_3 + O$	0	0	0	0	3.5	3.5	(3)
$O_3 + M \rightleftharpoons O + O_2 + M$	0	0	0	0	100	100	(3)
$O + M \rightleftharpoons O^+ + e^- + M$	0	0	0	0	0	0	(3)
$H + O_2 \rightleftharpoons OH + O$	0	0	0	0	0	0	(3)
$O + H_2 \rightleftharpoons OH + H$	0	0	0	0	0	0	(3)
$O + H_2O \rightleftharpoons 2OH$	100	100	100	100	100	100	(3)
$H_2O + M \rightleftharpoons OH + H + M$	0	0	0	---	---	---	(3)
$H_2O + H \rightleftharpoons H_2 + OH$	100	100	100	100	100	100	(3)
$H_2 + O_2 \rightarrow 2OH$	0	0	0	0	0	4.7	(3)
$OH + M \rightleftharpoons O + H + M$	0	0	0	---	---	---	(3)
$H_2 + O \rightleftharpoons H_2O$	100	100	100	100	100	100	(3)
$H + O_2 + M \rightleftharpoons HO_2 + M$	100	100	100	100	100	100	(3)

Table B - 3 Conversion of Nitrogen, and Ammonia Reaction in Percent for a Mass Flux of 0.01 lb per ft<sup>2</sup> sec.

Equation	500°F	1000°F	1500°F	2000°F	2500°F	3000°F	Comment
N <sub>2</sub> + M ⇌ 2N + M	0	0	0	0	0	0	(3)
2NO ⇌ NO <sub>2</sub> + N	0	0	0	0	0	1.3	(3)
2NO ⇌ N <sub>2</sub> + O <sub>2</sub>	0	0	0	0	0	1.1	(3)
NO + M ⇌ N + O + M	0	0	0	---	---	---	(3)
NO <sub>2</sub> + M ⇌ NO + O + M	0	0	0	0	100	100	(3)
N <sub>2</sub> O ⇌ N <sub>2</sub> + 1/2 O <sub>2</sub>	0	0	0	47.0	100	100	(3)
N <sub>2</sub> O + M ⇌ N <sub>2</sub> + O + M	0	0	0	0	0	3.5	(3)
N <sub>2</sub> O + O ⇌ N <sub>2</sub> + O <sub>2</sub>	3.4	62.0	90.0	95.7	97.4	98.1	(3)
N <sub>2</sub> O + O ⇌ 2NO	0	71.5	99.1	100	100	100	(3)
NO + O ⇌ O <sub>2</sub> + N	0	0	0	0	0	0	(3)
NO + N ⇌ N <sub>2</sub> + O	100	100	100	100	100	100	(3)
NO + O <sub>2</sub> ⇌ NO <sub>2</sub> + O	0	0	0	0.7	7.4	30.3	(3)
NO + N <sub>2</sub> ⇌ N <sub>2</sub> O + N	0	0	0	0	0	0	(3)
NO + N <sub>2</sub> O ⇌ NO <sub>2</sub> + N <sub>2</sub>	0	0	0.6	27.8	85.6	95.0	(3)
NO <sub>2</sub> + O <sub>2</sub> ⇌ N <sub>2</sub> + O <sub>2</sub> + O	0	0	0	0	0	0	(3)
NO <sub>2</sub> + O <sub>2</sub> ⇌ NO + O <sub>3</sub>	0	0	0.9	54.1	100	100	(3)
NO <sub>3</sub> + M ⇌ NO <sub>2</sub> + O + M	0	0	0	0	0	0	(3)

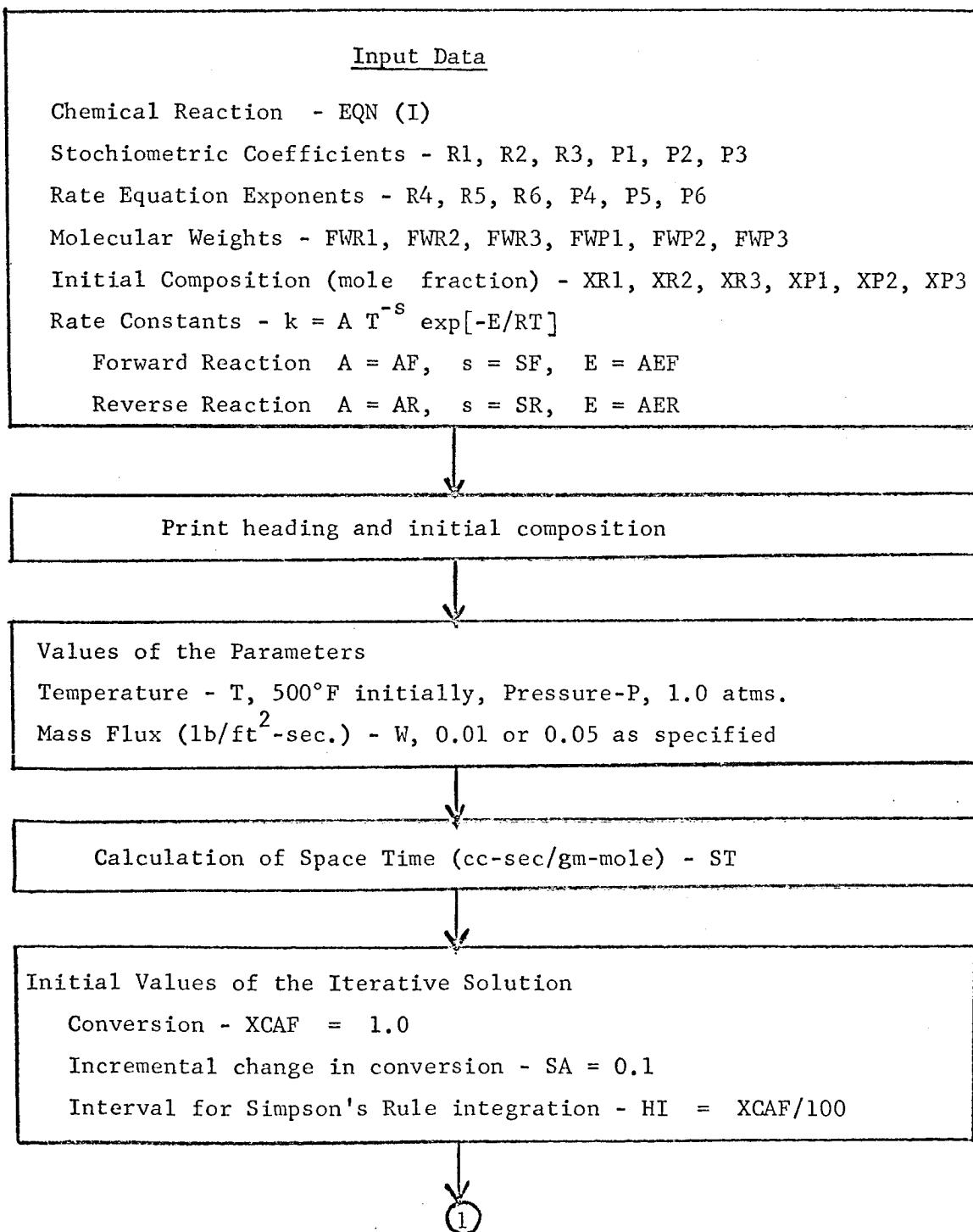
Table B-3 Continued

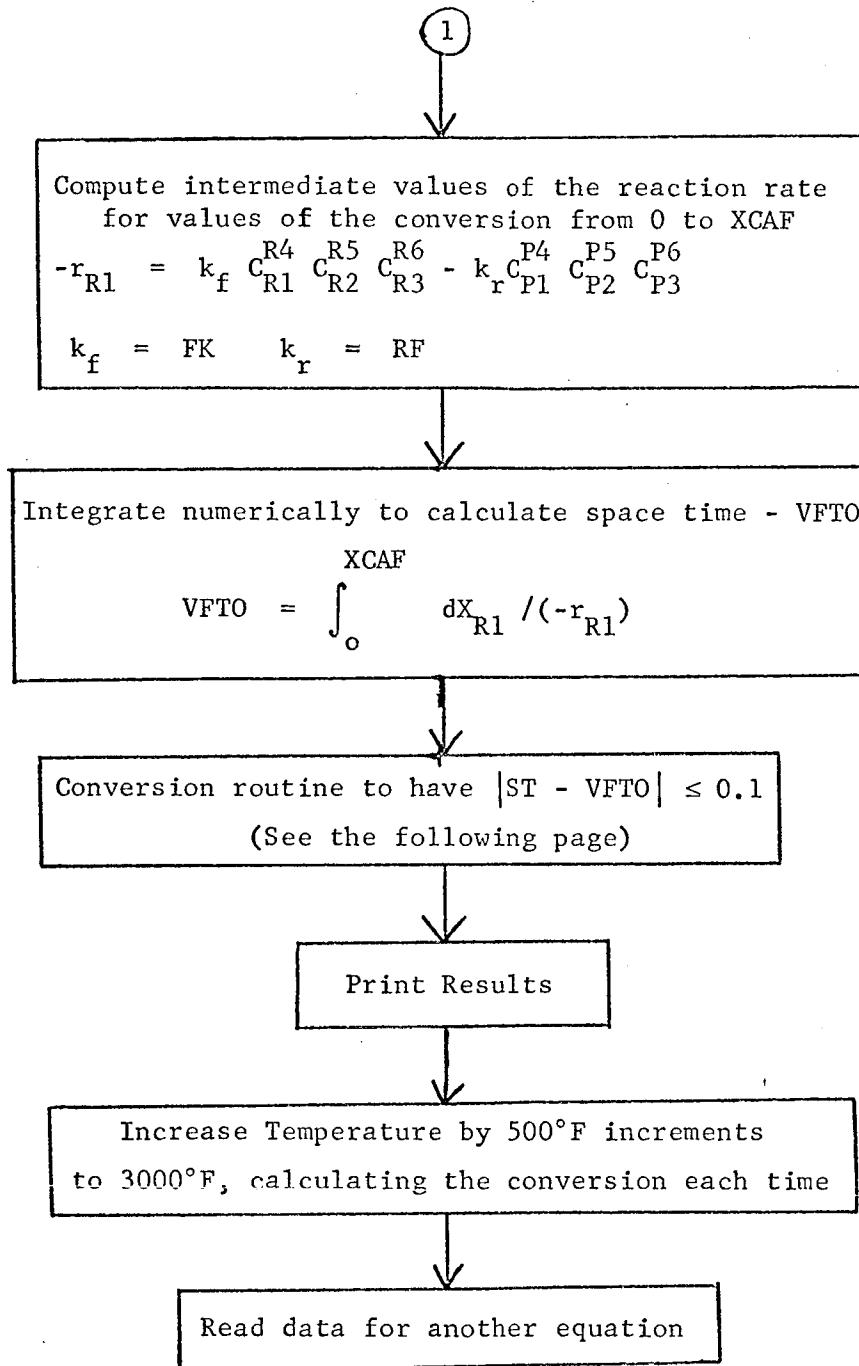
Equation	500°F	1000°F	1500°F	2000°F	2500°F	3000°F	Comment
H + N <sub>2</sub> O ⇌ N <sub>2</sub> + OH	98.4	100	100	100	100	100	(3)
NH <sub>3</sub> (g) + C(s) ⇌ HCN(s) + H <sub>2</sub> (g)	0	0	0	0	0	0	(3)
NH <sub>3</sub> ⇌ 1/2 N <sub>2</sub> + 3/2 H <sub>2</sub>	0	0	0	0	0	0.6	(3)
NH <sub>3</sub> + 5/2 O ⇌ 3/2 H <sub>2</sub> O + NO	100	100	100	100	100	100	(3)
N + M ⇌ N <sup>+</sup> + e <sup>-</sup> + M	0	0	0	0	0	0	(3)
N + NO ⇌ N <sub>2</sub> + O <sup>+</sup> + e <sup>-</sup>	0	0	0	0	0	0	(3)
N <sub>2</sub> <sup>+</sup> + e <sup>-</sup> ⇌ 2N	100	100	100	100	100	100	(3)
N <sub>2</sub> <sup>+</sup> + N ⇌ N <sub>2</sub> + N <sup>+</sup>	0	0	0	0	0	0	(3)
O <sub>2</sub> <sup>+</sup> + e <sup>-</sup> ⇌ 2O	100	100	100	100	100	100	(3)

Table B-4 Conversion of Carbon, Hydrocarbon, and Oxygen Reaction in Percent for a Mass Flux of  
0.01 lb per ft<sup>2</sup> sec

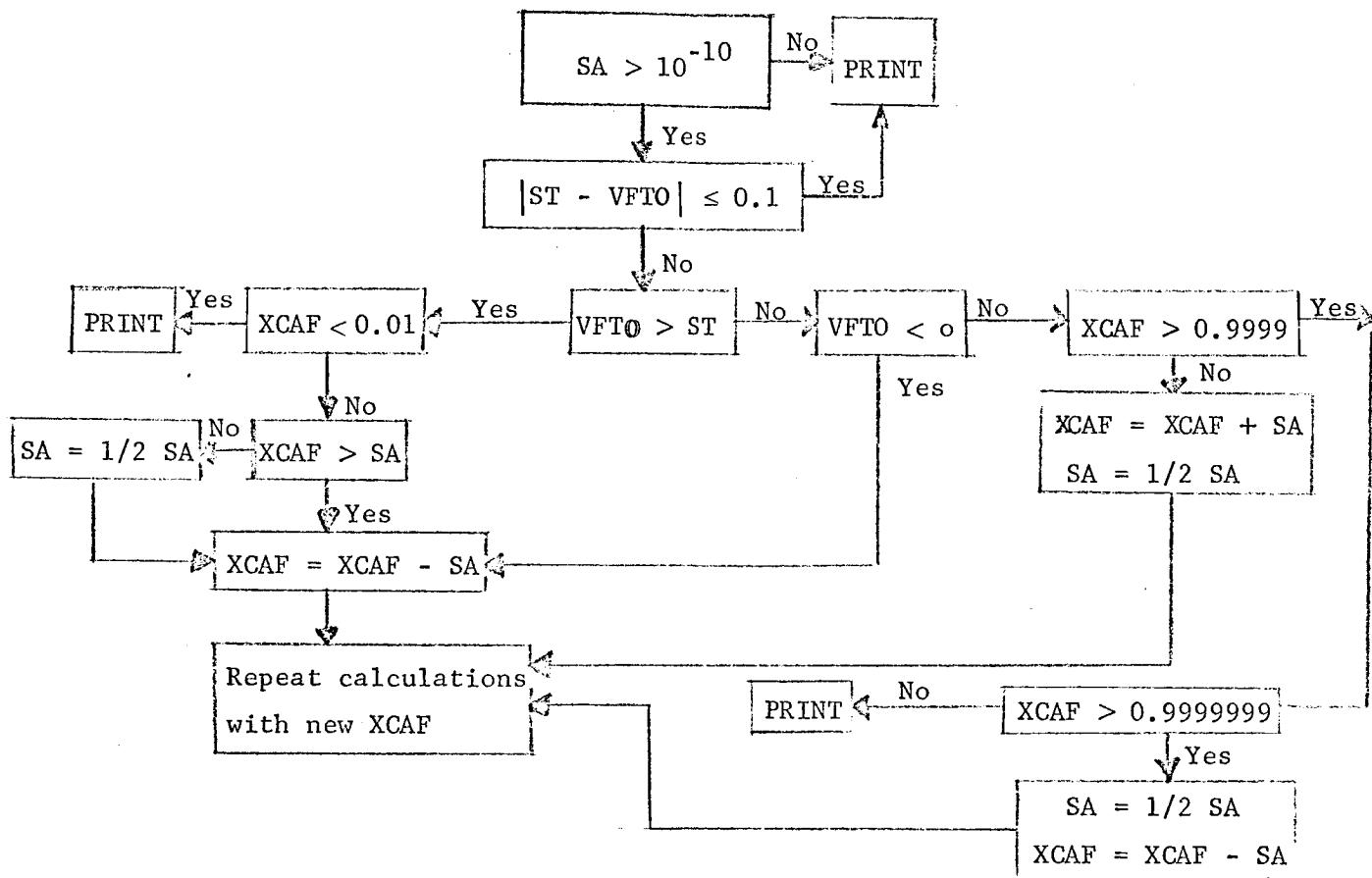
Equation	500°F	1000°F	1500°F	2000°F	2500°F	3000°F	Comment
C(s) + CO <sub>2</sub> (g) ⇌ 2CO	0	0	0	55.6	100	100	(3)
CO <sub>2</sub> + M ⇌ CO + O + M	0	0	0	0	4.9	100	(3)
CH <sub>4</sub> + O <sub>2</sub> → (CO, CO <sub>2</sub> , H <sub>2</sub> O, CH <sub>2</sub> O, ...)	0	0	20.2	59.3	78.0	---	(3)
CH <sub>4</sub> + O <sub>2</sub> → (CO, CO <sub>2</sub> , H <sub>2</sub> O, CH <sub>2</sub> O, ...)	1.0	57.6	86.5	93.2	95.5	---	(3)
CH <sub>4</sub> + O + M → CO, CO <sub>2</sub> , H <sub>2</sub> O, CH <sub>2</sub> O ...	0	0	0	0	0	0	(3)
C <sub>3</sub> O <sub>2</sub> → C(s) + 2CO	0	7.0	100	100	100	100	(3)
CO + OH ⇌ H + CO <sub>2</sub>	100	100	100	100	100	100	(3)
CH <sub>4</sub> + OH ⇌ CH <sub>3</sub> + H <sub>2</sub> O	100	100	100	100	100	100	(3)

Figure B-1. Flow Diagram of the Computer Program  
to Compute the Conversion of a Chemical Reaction  
Occurring in the Char Zone Isothermally





#### Conversion Routine



\$IBFTC MAIN  
 C NASA PROJECT NC. 135-30-8621  
 C CALCULATION OF THE CONVERSION FOR CHEMICAL REACTIONS  
 C THAT POSSIBLY OCCUR IN THE DECOMPOSITION ZONE OF  
 C CHARRING ABLATORS. THE RESULTS COMPUTED ARE FOR THE  
 C ISOTHERMAL FLOW IN THE CHAR ZONE AT TEMPERATURES  
 C FROM 500.0-OF TO 3000.0-OF  
 C NASA GRANT NGR-19-001-016  
 C EVALUATION OF THE ENERGY TRANSFER IN THE CHAR ZONE DURING ABLATION  
 C PROJECT NUMBER 1303 53067  
 C  
 C DIMENSION Y(150), EQN(150)  
 C  
 C READ THE EQUATION R1+R2+R3=P1+P2+P3  
 1111 READ729,(EQN(I),I=1,12)  
 729 FORMAT(12A6)  
 C  
 C READ THE STOCHIOOMETRIC COEFFICIENTS OF THE RATE EQUATION  
 READ730,R1,R2,R3,P1,P2,P3  
 C  
 C READ EXPONENTS ON THE COMPOSITIONS OF THE RATE EQUATION  
 READ 730,R4,R5,R6,P4,P5,P6  
 730 FORMAT(6F4.0)  
 C  
 C READ THE MOL WGT OF THE COMPONENTS  
 READ731,FWR1,FWR2,FWR3,FWP1,FWP2,FWP3  
 731 FORMAT(6F5.0)  
 C  
 C READ THE INITIAL COMPOSITION OF THE REACTANTS IN MOLE FRACTION  
 READ5,XR1,XR2,XR3,XP1,XP2,XP3  
 5 FORMAT(6E10.0)  
 C  
 C READ THE COEFFICIENTS OF THE FORWARD REACTION RATE CONSTANT  
 C UNITS OF AF ARE IN CUBIC-CM, GM-MOLE AND SEC  
 C UNITS OF AEF ARE IN KCAL PER GM-MOLE  
 READ733,AF,SF,AEF  
 733 FORMAT(E8.0,2F6.0)  
 C  
 C READ THE COEFFICIENTS OF THE REVERSE REACTION RATE CONSTANT  
 C UNITS OF AR ARE IN CUBIC-CM, GM-MOLE AND SEC  
 C UNITS OF AER ARE IN KCAL PER GM-MOLE  
 READ733,AR,SR,AER  
 C  
 828 PRINT829,(EQN(I),I=1,12)  
 829 FORMAT(1H1,12A6)  
 PRINT 830  
 830 FORMAT(1X,35HINITIAL COMPOSITION (MOLE FRACTION))  
 PRINT 833,XR1,XR2,XR3,XP1,XP2,XP3

```

C PRINT 831
831 FORMAT(1HC,105HFINAL COMPOSITION (MOLE FRACTION)
1 TEMP FRACTIONAL SP.TIME(CC-SEC/MOL) REACTION RATE )
PRINT 8311
8311 FORMAT(1F ,105H R1 R2 R3 P1 P2 P3
1 (OF) CONVERSION COMPUTED SPECIFIED (MOL/CC-SEC) )

C MASS FLUX OF DECOMPOSITION PRODUCTS, W, IN LB/FT2-SEC
W=0.01

C INITIAL VALUE OF TEMPERATURE,T, IS 500-OF
T=500.
C INITIAL VALUE OF THE PRESSURE ,P, IS 1.0 ATMS
P=1.0
C GAS CONSTANT,R, IN CALORIES/GMMOLE-OK
R=1.987

C CALCULATION OF THE AVERAGE MOL WGT OF THE GAS,FWA
C ENTERING THE CHAR ZONE
FWAR=FWR1*XRI+FWR2*XR2+FWR3*XR3
FWAP=FWP1*XP1+FWP2*XP2+FWP3*XP3
FWA=FWAR+FWAP

C CALCULATION OF THE MOLAL FLOW RATE OF THE GAS,FTO
C FTO HAS UNITS OF GMMOLES PER FT-FT SEC
FTO=(454.0*W)/FWA

C CALCULATION OF MOLAL FLUX OF THE INDIVIDUAL COMPONENTS
C MOLAL FLUX UNITS ARE GMMOLES PER FT-FT SEC
FR10=XRI*FTO
FR20=XR2*FTO
FR30=XR3*FTO
FP10=XP1*FTO
FP20=XP2*FTO
FP30=XP3*FTO

C CALCULATION OF THE SPACE TIME,ST, IN CUBIC-CM SEC/GMMOLES
ST=(0.25*144.0)/(FTO*0.06103)

C CONVERSION OF 100 PERCENT IS ASSUMED INITIALLY
C XCAF IS THE CONVERSION OF COMPONENT A, INITIALLY 1.0
XCAF=1.0
C NO CONVERSION OF PRODUCTS INITIALLY
XCA=0.0
C INITIAL INCREMENTAL CHANGE,SA, OF THE CONVERSION XCAF
SA=0.1

C CALCULATION OF SPACE TIME FOR AN ASSUMED CONVERSION,XCAF.
C REPEAT CALCULATIONS UNTIL CALCULATED SPACE TIME IS EQUAL
C TO THE KNOWN VALUE. THIS DETERMINES THE CORRECT VALUE
C OF THE FINAL CONVERSION

C FIRST
C DETERMINE CONCENTRATION OF COMPONENTS FOR VARIOUS
C INTERMEDIATE CONVERSIONS,XCA.CONCENTRATION ARE
C IN GM-MOLE/CUBIC-CM
C INCREMENTAL CHANGE IN XCA IS HI
2222 HI=XCAF/100.0

```

C XCA=C.0

C CC1 I=1,101

C C F/S ARE MOLAL FLUXES CORRESPONDING TO CONVERSION XCA  
C C MOLAL FLUXES HAVE UNITS OF GM/MOLE/FT-FT SEC

C FR1=(1.0-XCA)\*FR10  
FR2=FR20-(FR10\*XCA\*R2)/R1  
FR3=FR30-(FR10\*XCA\*R3)/R1  
FP1=FP10+(FR10\*XCA\*P1)/R1  
FP2=FP20+(FR10\*XCA\*P2)/R1  
FP3=FP30+(FR10\*XCA\*P3)/R1

C C THE TOTAL MOLAL FLUX CORRESPONDING TO CONVERSION XCA IS FT  
C FT HAS UNITS OF CM-MOLES/FT-FT-SEC  
FT=FT0+(FR10\*XCA)\*(P1+P2+P3-R1-R2-R3)/R1

C C CALCULATION OF THE COMPOSITION OF THE REACTING MIXTURE  
C C S ARE CONCENTRATIONS IN GM/MOLE/CUBIC-CM

RR=82.054  
TCK=(T+460.0)/1.8  
H=P/(RR\*TCK\*FT)  
CR1=FR1\*H  
CR2=FR2\*H  
CR3=FR3\*H  
CP1=FP1\*H  
CP2=FP2\*H  
CP3=FP3\*H

C C CALCULATION OF RATE CONSTANTS FOR FORWARD AND REVERSE REACTIONS  
C RATE CONSTANT UNITS ARE IN CUBIC CM, GM/MOLE AND SEC

C C FORWARD REACTION RATE CONSTANT, FK  
FK=AF\*TOK\*\*(-SF)\*EXP((-AEF\*1000.0)/(R\*TOK))

C C REVERSE REACTION RATE CONSTANT, RK  
RK=AR\*TOK\*\*(-SR)\*EXP((-AER\*1000.0)/(R\*TOK))

C C CALCULATION OF REACTION RATE, RA, OF COMPONENT A  
C RA HAS UNITS OF GM/MOLE/CUBIC-CM SEC  
RA=FK\*(CR1\*\*R4)\*(CR2\*\*R5)\*(CR3\*\*R6)-RK\*(CP1\*\*P4)\*(CP2\*\*P5)\*  
1(CP3\*\*P6)

C C CALCULATION OF FUNCTION UNDER INTEGRAL-1/RA=Y(I)  
Y(I)=1.0/RA

1 XCA=XCA+HI

C STEP XCA TO GENERATE 101 VALUES OF Y(I)

C CALCULATION OF FINAL COMPOSITION (MOLE FRACTION)

YR1=FR1/FT

YR2=FR2/FT

YR3=FR3/FT

YP1=FP1/FT

YP2=FP2/FT

YP3=FP3/FT

C C CALCULATION OF SPACE TIME FOR THE SPECIFIED CONVERSION, XCAF

```

C INTEGRATION IS PERFORMED USING SIMPSONS RULE
SUM1=0.0
SUM2=0.0
DC2 I=2,100
2 SUM1=2.0*Y(I)+SUM1
DC3 I=2,100,2
3 SUM2=2.0*Y(I)+SUM2
C INTEGRAL VALUE IS VINT-UNITS ARE CUBIC-CM SEC/GMMOLES OF A
VINT=(HI/3.0)*(Y(1)+SUM1+SUM2+Y(101))
C SPACE TIME CALCULATED IS VFT0-UNITS ARE CUBIC-CM SEC/GMMCLES
VFT0=XR1*VINT
C
C
C COMPUTATION STOPS IF SA IS LESS THAN 1.0E-10
IF(SA.GT.1.0E-10)GO TO 777
GO TC 123
777 CONTINUE
C DETERMINE IF THE DIFFERENCE BETWEEN THE SPECIFIED AND
C CALCULATED SPACE TIME IS WITHIN 0.1. IF YES INCREASE THE
C TEMPERATURE BY 500-OF
CALL SSWTCH(1,JOB)
GO TC (1111,778),JOB
778 IF(ABS(ST-VFT0).LT.0.1) GO TO 123
C
C DETERMINE IF VFT0 IS GREATER THAN ST
IF(VFT0.GT.ST)GOTO1234
C
C VFT0 IS LESS THAN ST
C
C IS VFT0 NEGATIVE
C YES-REDUCE XCAF
C NO-CONTINUE
IF(VFT0.LT.0.0) GO TO 1321
C
C THE CALCULATION STOPS IF THE CONVERSION IS GREATER THAN 99.99 PERCENT
IF(XCAF.GT.0.9999)GO TO 321
C
C THE PREVIOUS VALUE OF VFT0 IS RECALCULATED BY INCREASING
C XCAF BY THE AMOUNT OF SA
C THEN CHANGE SA TO 0.5*SA
XCAF=XCAF+SA
SA=0.5*SA
GOTO 2222
C
C CHECK TO INSURE XCAF IS LESS THAN 1.0
321 IF(XCAF.GT.0.999999)GO TO 112
GOTO123
112 SA=0.5*SA
XCAF = XCAF - SA
GO TC 2222
C
C VFT0 IS GREATER THAN ST
C
C THE CALCULATION STOPS IF THE CONVERSION IS LESS THAN 0.05 PERCENT
1234 IF(XCAF.LE.0.01)GOTO123
C
C
C A CHECK TO PREVENT XCAF - SA = 0
1321 IF(XCAF.GT.SA) GO TO 4321

```

C  
C SA = 0.5\*SA

C  
C THE VALUE OF XCAF IS REDUCED BY THE VALUE OF SA  
4321 XCAF=XCAF-SA

C  
C THEN THE CALCULATION IS REPEATED TO DETERMINE A  
C NEW SPACE TIME FOR COMPARISON

C  
C GO TO 2222

C  
C VFTG IS ESSENTIALLY EQUAL TO ST (WITHIN 0.1)

C  
C OR

C CONVERSION, XCAF, IS LESS THAN 0.5 PERCENT

C  
C OR

C CONVERSION, XCAF, IS GREATER THAN 99.99 PERCENT

C PRINT THE RESULTS

123 PRINT 833,YR1,YR2,YR3,YP1,YP2,YP3,T,XCAF,VFTG,ST,RA

833 FORMAT(1HC,6F8.4,F9.1,F8.4,3E12.5)

C  
C READ NEW DATA IF THE CONVERSION IS 100 PERCENT  
C CONVERSICN WILL BE 100 PERCENT FOR ALL HIGHER TEMPERATURES  
IF(XCAF.GT.0.99) GO TO 2208

C  
C THEN REPEAT THE CALCULATIONS AT THE NEW TEMPERATURE

C  
C INCREASE THE TEMPERATURE BY 500-OF  
T=T+500.

C  
C RESET XCAF AND SA

SA = 0.1

XCAF=1.0

C  
C IF THE TEMPERATURE IS LESS THAN OR EQUAL TO 7000-OF  
C CONTINUE THE CALCULATION  
IF(T.LE.7000.0)GOTO 2222

C  
C PRINT DATA

2208 PRINT 2209,W

2209 FORMAT(1H-,25H MASS FLUX(LB/FT2-SEC) = , F8.4)

PRINT2210,AF,SF,AEF

2210 FORMAT(1HC,3HAF=,E9.2,5H SF=,F6.2,6H AEF=,F6.1)

PRINT2211,AR,SR,AER

2211 FORMAT(1H0,3HAR=,E9.2,5H SR=,F6.2,6H AER=,F6.1)

PRINT2212

2212 FORMAT(1H0,29HFWR1 FWR2 FWR3 FWP1 FWP2 FWP3)

PRINT2213,FWR1,FWR2,FWR3,FWP1,FWP2,FWP3

2213 FORMAT(1H0,6F6.1)

PRINT 2218

2218 FORMAT(1H0,28H STOCHIOMETRIC COEFFICIENTS)

PRINT2214

2214 FORMAT(1HC,24H R1 R2 R3 P1 P2 P3)

PRINT2215,R1,R2,R3,P1,P2,P3

2215 FORMAT(1H0,6F4.1)

PRINT 2219

2219 FORMAT(1H0,45H EXPONENTS ON THE COMP. OF THE RATE EQUATION)

PRINT 2216

2216 FORMAT(1H0,24H R4 R5 R6 P4 P5 P6)

PRINT 2217,R4,R5,P4,P5,P6

2217 FORMAT(1H0,6F4.1/1H1)  
C READ IN NEW DATA FOR CALCULATIONS OF NEXT EQUATION

GOTO111

24 STOP

END

\$ENTRY

C & CC2 = 2CD  
INITIAL COMPOSITION (MOLE FRACTION)

0.5000 0.5000 0.0000 0.0000 0.0000 0.0000

FINAL COMPOSITION (MOLE FRACTION)  
R1 R2 R3 P1 P2 P3

	R1	R2	R3	P1	P2	P3	TEMP (OF)	FRACTIONAL CONVERSION	SP. TIME(CC-SEC/MOL) COMPUTED	REACTION RATE SPECIFIED (MOL/CC-SEC)
0.4969	0.4969	0.0000	0.0062	0.0000	0.0000	0.0000	500.0	0.0062	0.14224E 23	0.36380E 04
0.4969	0.4969	0.0000	0.0062	0.0000	0.0000	0.0000	1000.0	0.0062	0.16729E 11	0.36380E 04
0.4969	0.4969	0.0000	0.0062	0.0000	0.0000	0.0000	1500.0	0.0062	0.24013E 05	0.36380E 04
0.0000	0.0000	0.0000	1.0000	0.0000	0.0000	0.0000	2000.0	1.0000	0.13083E 04	0.36380E 04

MASS FLUX(LB/FT<sup>2</sup>-SEC) = 0.0100

AF= 0.15E 11 SF= 0.00 AEP= 85.0

AR= 0.10E-29 SR= 0.00 AER= 0.0

FWR1 FWR2 FW3 FW1 FW2 FW3

12.0 44.0 0.0 28.0 0.0 0.0

STOCHIONETRIC COEFFICIENTS

R1 R2 R3 P1 P2 P3

1.0 1.0 0.0 2.0 0.0 0.0

EXPCNENTS ON THE CNMP. OF THE RATE EQUATION

R4 R5 R6 P4 P5 P6

0.0 0.0 0.0 0.0 0.0 0.0

## APPENDIX C

TEMPRE - PROGRAM FOR THE SOLUTION OF  
THE FROZEN FLOW, EQUILIBRIUM AND NON-EQUILIBRIA  
FLOW MODELS

The program for the solution of the frozen flow, equilibrium and non-equilibrium flow cases is composed of several individually tested programs written in Fortran IV for the IBM 7040 computer. These are labeled TEMPRE, PROPT, OMEGA, CHAR, MOLFRA, MATINV AND KINET, represented in Figures C1-C5 . The specific function of each will be discussed in detail in the following section.

TEMPRE

This program forms the core of the entire system. All common input information required by the system is channeled through TEMPRE to the specific subprograms. The main function of TEMPRE is to calculate the temperature distribution using a fourth order Runge-Kutta analysis which includes the convergence sequence used in determining the initial slope needed to produce a valid profile.

A second portion of TEMPRE is used to calculate the pressure distribution and heat flux within the char zone. Simpson's Rule is used to evaluate integrals in the pressure distribution and heat flux equations. Subprogram OMEGA is used as an interpolation program to first calculate the viscosity of the gas mixture from the collision integral table and secondly to interpolate from the temperature distribution (previously generated in TEMPRE) for values corresponding to a specific char depth.

PROPT

This is the first major subprogram which calculates the physical property data for the gases as functions of temperature (heat capacity, thermal conductivity, change in thermal conductivity with temperature). Information is retrieved from PROPT at each temperature interval generated in the Runge-Kutta analysis in TEMPRE. Subprogram PROPT depends on OMEGA for the value of the collision integral necessary in calculating the gas physical properties and CHAR for the value of the char thermal conductivity.

OMEGA

This is the first minor subprogram which calculates the collision integral for a pure gas at a specified temperature level. An  $n^{\text{th}}$  order Lagrangian interpolation procedure is used to select the value from a table containing the collision integral as a function of temperature and the pure gas in question.

CHAR

This minor subprogram fits a curve to available char thermal conductivity data for use in calculating an effective conductivity value. Any curve fitting method which best describes the given data can be used.

The above programs comprise the system for the frozen flow model. Extension to include the equilibrium flow model is accomplished by the addition of MOLFRA AND MATINV, while the non-equilibrium flow model requires the addition of KINET to the frozen flow programs.

MOLFRA

This is the second major subprogram which is used to determine the

equilibrium gas composition (in term of mole fractions), average molecular weight, net change in the total molar flux, and reaction rate expression as functions of temperature. The procedure involves the minimization of the free energy at various tabulated temperature levels. Transfer of data from MOLFRA to TEMPRE is accomplished using OMEGA as an interpolation method.

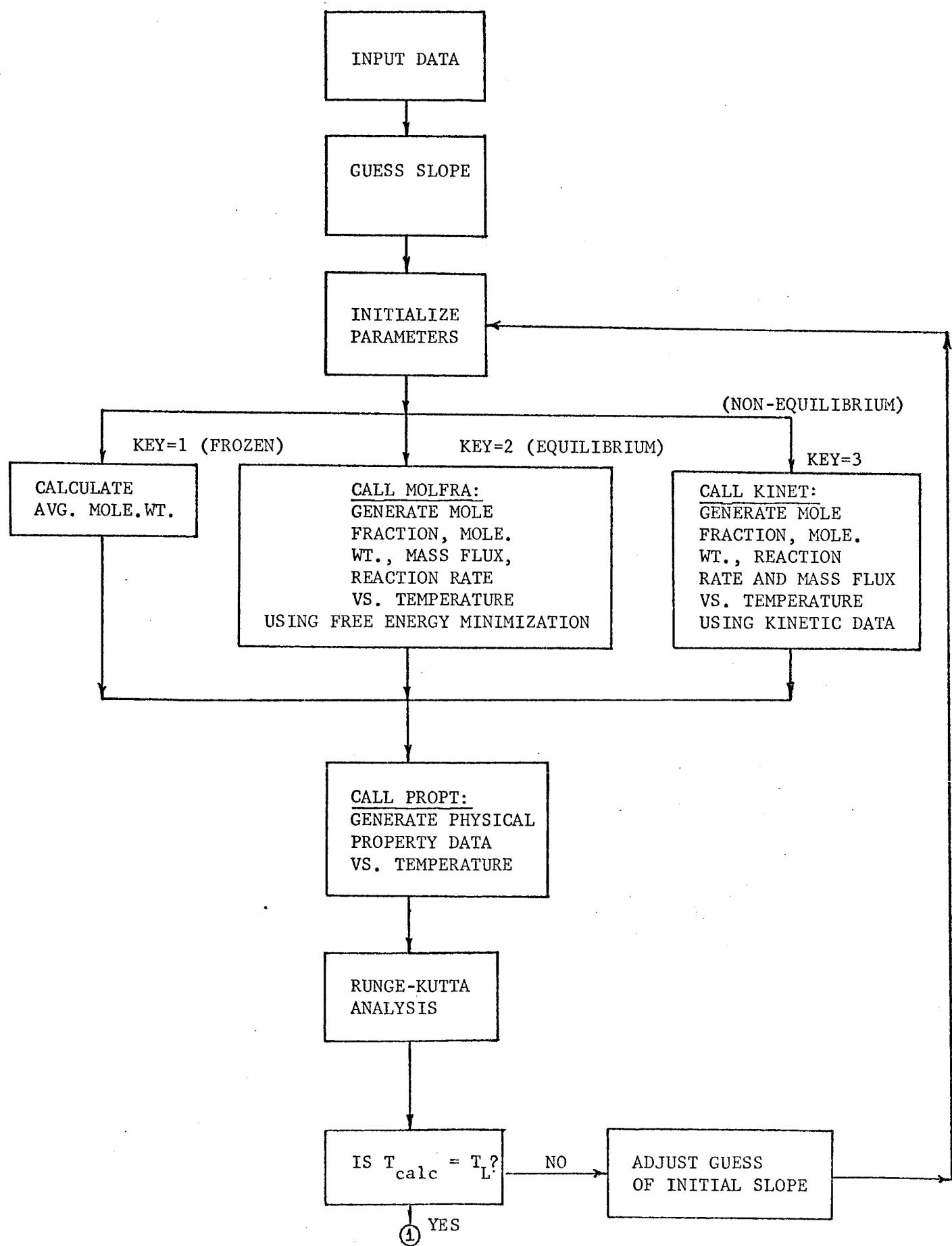
#### MATINV

This minor subprogram is used to find the inverse of a non-singular  $N \times N$  matrix. The inversion is performed iteratively by reducing the original matrix to an identity matrix by a sequence of row operations followed by applying the same operation to the identity matrix to generate the inverse.

#### KINET

This is the third major subprogram which estimates the composition (in terms of mole fractions), average mole weight, mass flux and reaction rate as a function of temperature supplied from TEMPRE. The procedure utilizes the kinetic data of pertinent chemical reactions that occur in the char zone. Transfer of data for the temperature profile is accomplished in the argument of the call statement. After calculation of the correct temperature profile pertinent data is retrieved from KINET using OMEGA, the interpolation subprogram.

FIGURE C 1  
TEMPRE-PROGRAM FOR THE CALCULATION OF THE TEMPERATURE-PRESSURE PROFILES AND THE HEAT FLUX AT THE SURFACE IN THE CHAR ZONE OF A CHARRING ABLATOR



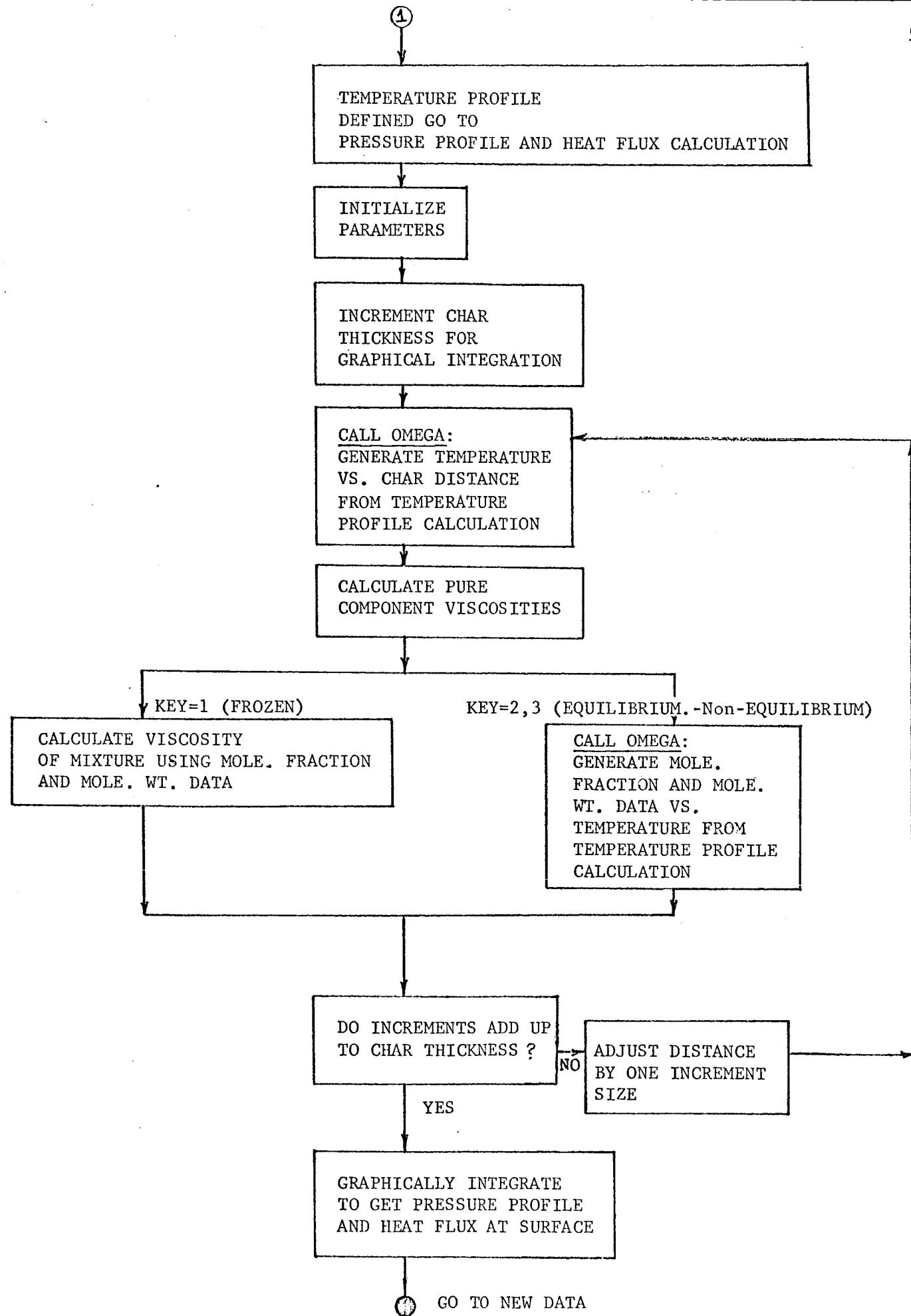


Figure C 2  
PROPT - SUBPROGRAM FOR CALCULATING  
PHYSICAL PROPERTY DATA

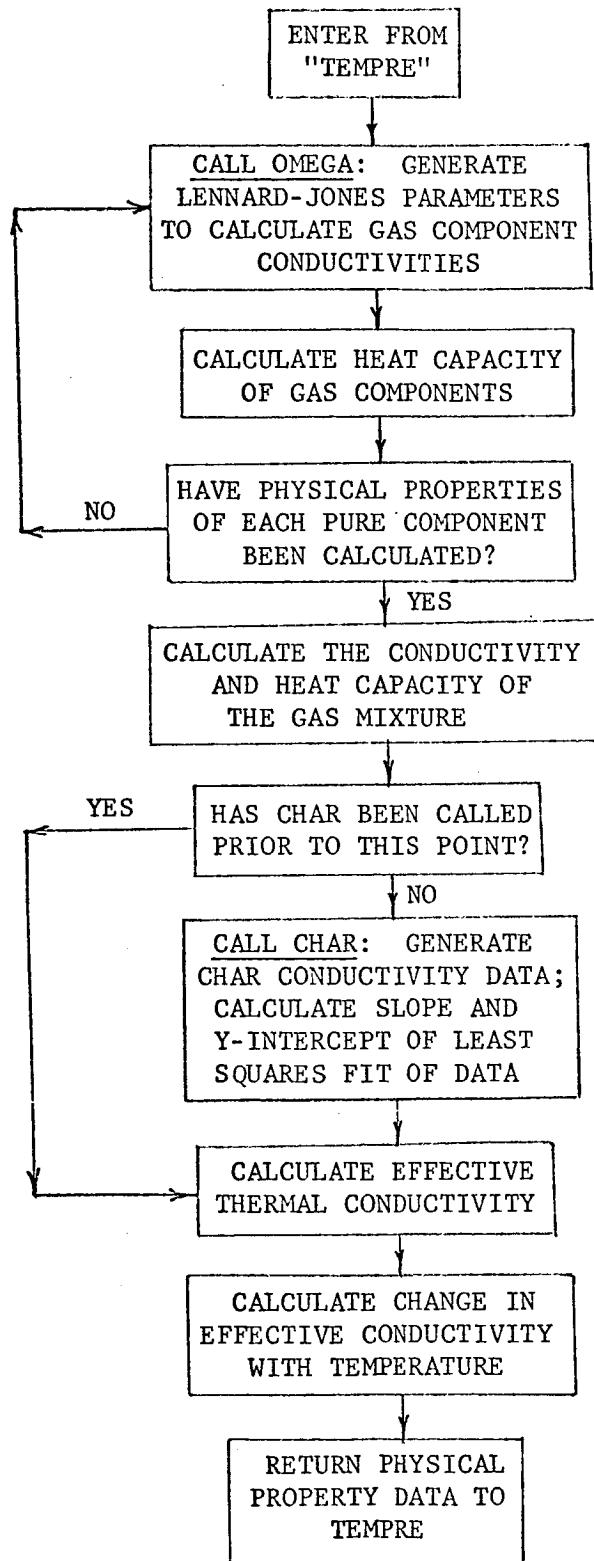
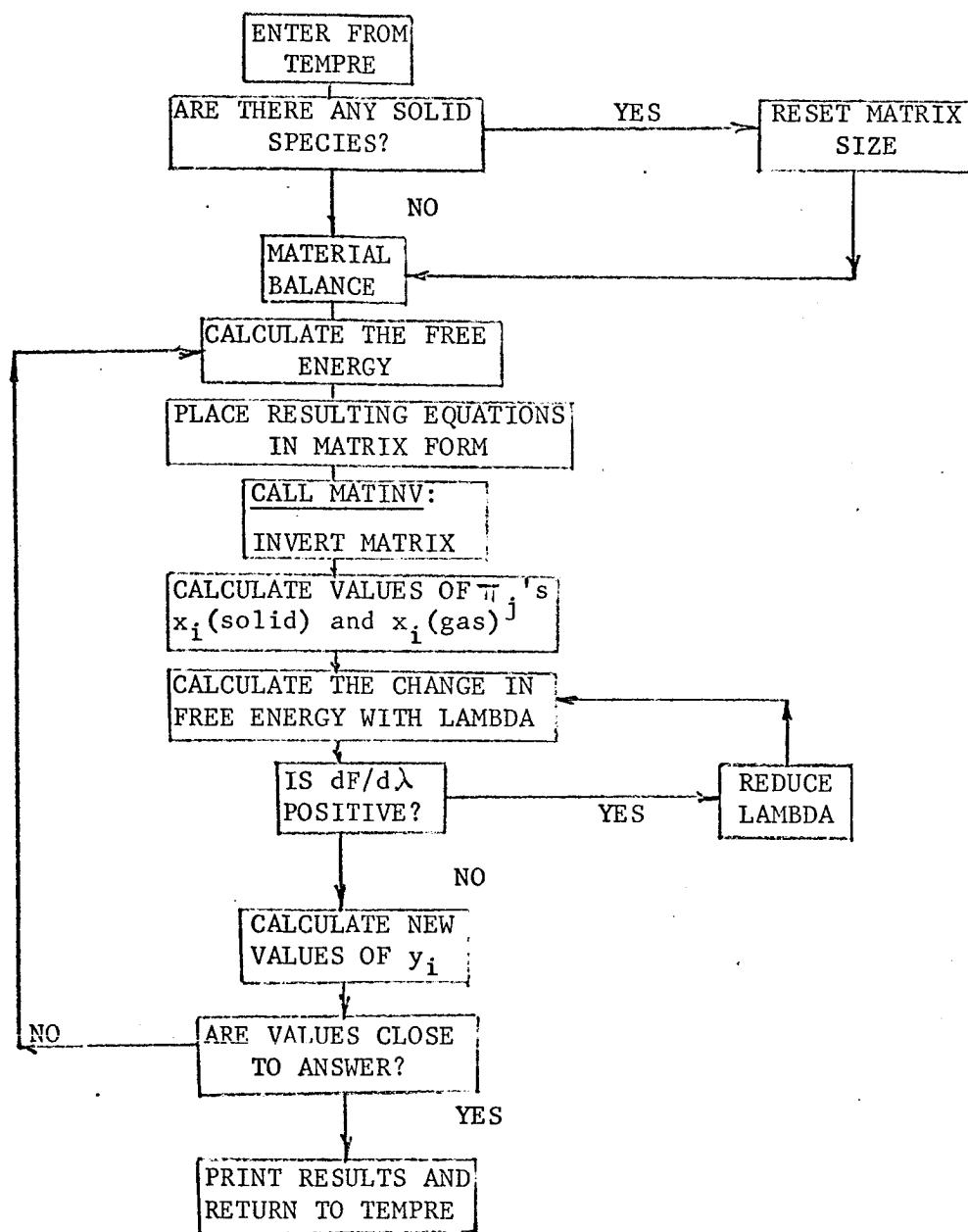


Figure C 4

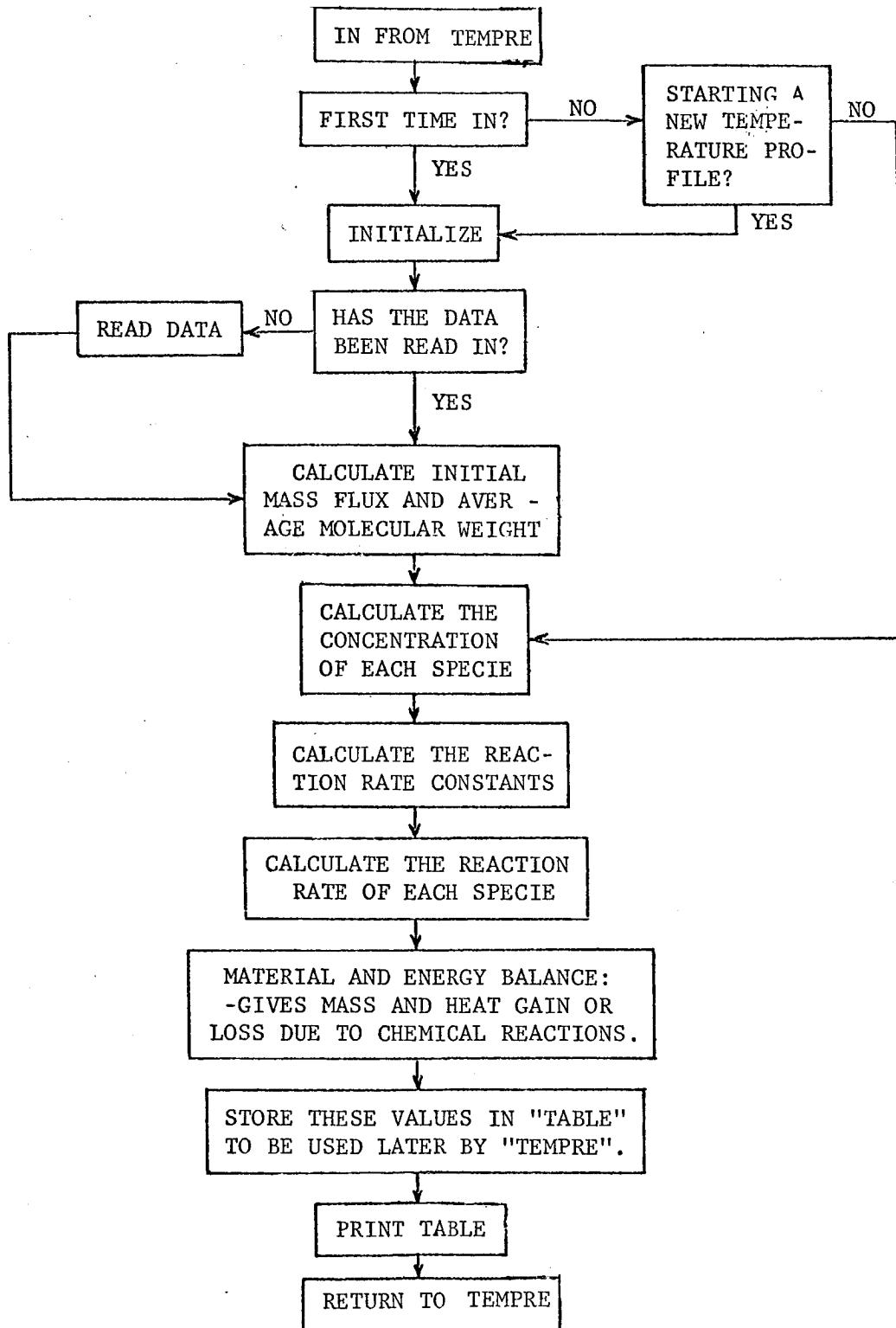
MOLFRA - SUBPROGRAM FOR THE CALCULATION OF MOLE FRACTIONS, AVERAGE MOLECULAR WEIGHT, MASS FLUX, AND HEAT OF REACTION VALUES VS. TEMPERATURE BY A FREE ENERGY MINIMIZATION METHOD



MATINV - SUBPROGRAM TO INVERT THE MATRIX FORMED IN MOLFRA

(STANDARD MATRIX INVERSION COMPUTER PROGRAM)

Figure C 5  
 "KINET"-- SUBROUTINE FOR THE CALCULATION OF THE  
 RATE OF REACTION, MASS FLUX, AVERAGE MOLECULAR  
 WEIGHT AND HEAT GENERATED DUE TO CHEMICAL REACTIONS





## FORTRAN SOURCE LIST TEXPRE

## SOLVED EQUATIONS

1e THERM(1,1,1)  
 2e THERMUS COEFFICIENT IN Darcy equation (1/EF)  
 3e THERMUS COEFFICIENT IN Darcy equation (1/ET2)  
 4e THERMUS, MOLAR  
 5e THERMUS, DT(XTE) VS, ZONE DATA POINTS  
 6e THERMUS, OF CONSTANCED LOCATIONS FOR EQUILIBRIUM PROGRAM CALCULATIONS  
 7e THERMUS, OF CONSTANCED LOCATIONS FOR TEMPERATURE-DISTANCE CALCULATIONS  
 8e THERMUS, OF CONSTANCED LOCATIONS FOR PHYSICAL PROPERTY CALCULATIONS  
 9e THERMUS, OF CONSTANCED LOCATIONS FOR SUBPROGRAM OMEGA  
 KEY=1 (FREEZE FLOW), = 2 (EQUILIBRIUM FLOW) = 3 (NON-EQUILIBRIUM FLOW)  
 KDATA,INDX1,INDX2,INDX3,KEY  
 KTEMP,REDUCE OF TEMPERATURE AND ZICK VALUE  
 LDATA=CELLUSIC; INTEGRAL FACIALIZED VS XTE  
 RDATA,(KEY(1),ZING(1),I=1,NDATA)

22 FC=0.0(2500,5)  
 22 FC=1.0(514)  
 24 H=0.0002(15,5)  
 JCP=1  
 JEL  
 26 Z(1)=1.0  
 T(1)=TEMPERATURE AT Z=1 (OF)  
 T(1)=TEMPERATURE AT Z=1 (OF)  
 T(1)=TEMPERATURE GRADIENT AT Z=1 (OF/FT)  
 ZL=0.001 FT  
 TOLERANCE INCREMENT SIZE (FT)  
 MS=0.000001 FT, TOLERANCE SIZE (FT)  
 27 T(1)=T(1),T1,T2(1),ZL,I,MS,FT,HS  
 21 T(1)=T(1),T1  
 T1=0.0  
 C1=0.0,T1=0.0  
 123 S0=0.00017(1)  
 S0=0.00017(1)  
 127 Y1(1)=Y1(1)/SUM  
 Y1(1)=Y1(1)/SUM  
 CALL Y1(1,IP1,-1)  
 IP1=1  
 128 Y1(1)=Y1(1)  
 KOUNT=1  
 IP1=1(1)  
 K7=1  
 40 K=1  
 K=1  
 K=1  
 C0=1,I=1,NP  
 Y1(1)=Y1(1)  
 31 C0=1,I=1,NP  
 K=1  
 K=1  
 KOUNT=1  
 Y1(1)=Y1(1)  
 Y1(1)=Y1(1)  
 22 K=1,I=1,NP  
 23 K=(1-I)\*NP,I=1,NP  
 24 K=(1-I)\*NP,I=1,NP

## FORTRAN SOURCE LIST (EMPS)

## SOURCE STATEMENT

```

62  GROUP=(.5*EPS*GASCP/CDO)+(OCOO*DTC/CDO)+(REACT/CDO)
63  T0=6
64  GROUP=(.5*EPS*GASCP/CDO)+(OCOO*DTC/CDO)+(REACT/CDO)
65  DAE=DA+GROUP
66  DTC=TC+GROUP
67  TC=TC+T0
68  S0=TC(115,120,130,135),MX
69  A1=ARK
70  DA1=DA
71  TC=TC-A1
72  DTC=DTC-A1,5*DA1
73  NM=2
74  TF(TC)133,133,103
75  A2=ARK
76  DA2=DA
77  TC=TC-A2
78  DTC=DTC-A2,5*DA2
79  NM=3
80  TF(TC)133,133,103
81  A3=ARK
82  DA3=DA
83  TC=TC-A3
84  DTC=DTC-A3+DA3
85  NM=4
86  TF(TC)133,133,103
87  T0=TC(2222,TC)
88  FORMAT(1E0,3HTC=,1X,F15.6,8X,8HNEGATIVE)
89  DT(1)=DT(1)*1.5
90  GC  TC  40
91  A4=ARK
92  DA4=DA
93  T(1+1)=T(1)+(1.0/6.0)*(A1+2.0*A2+2.0*A3+A4)
94  DT(N+1)=DT(1)+(1.0/6.0)*(DA1+2.0*DA2+2.0*DA3+DA4)
95  T0=T0+1.4555555
96  TF(TC)=T0,0,OCOO,OCOO
97  PRINT 300,T(N+1),TLIMIT
98  PRINT 301,DT(N+1),N
99  FORMAT(1E0,7H(T(N+1)=,1X,F15.6,8X,8HNEGATIVE))
100  DT(1)=DT(1)*6.5
101  GC  TC  40
102  PRINT 300,T(N+1),TLIMIT
103  PRINT 301,DT(N+1),N
104  FORMAT(1E0,7H(T(N+1)=,1X,F20.5,8X,21H=,1X,I6)
105  TRATIO=(T0-T(N+1))/T0
106  DT(1)=T(1)*(1.0+0.5*TRATIO)
107  T0=DT(1)+T(N+1)
108  TF(TC)=T0,0,OCOO,40
109  Z(N+1)=Z(N)+H
110  XAXIS(N+1)=Z(N+1)/ZL
111  YAXIS(N+1)=(T(N+1)-T(1))/(T0-T(1))
112  TF(XAXIS(N+1),YAXIS(N+1))=,0,0,1,150,100,145
113  DT(1)=DT(N+1)
114  GC  TC  40
115  DT(N)=DT(N+1)

```

## FORTRAN SOURCE LIST EMPRE

## SOURCE STATEMENT

```

      CDT(1)=DT(1)
      CAPAC(1)=CAPAC(1)
      CDT=CDT(TL-T(N+1))
1111 PRINT(L111,T(1),DT(1))
1111 FORMAT(1H0,5H(T(1)=,1X,F15.6,4X,6HDT(1)=,1X,F15.6)
      STEP=(1.0*(ZLZ(1)+5.0))/10.0
      LSTEP=STEP
      LCHAR=LSTEP+1
      PRINT(100)
130  FORTRAN(1H0,3X,4HT(L),3X,5HOT(L),9X,BHXAXIS(L),7X,BHYAXIS(L),
      1      1X,BCAPAC(L),4X,1H)
      PD2=L-1,1CHAR
      PRINT(100,T(L),OT(L),XAXIS(L),YAXIS(L),CAPAC(L),L
130  ECAPAC(IX,5F13.5,15)
200  CONTINUE
      LE(CDTC-1,C)155,155,153
152  RATIO=(TL-OT(1))/OT(1)*1.0+0.9*RATIO
      OT(1)=OT(1)+RATIO
      FORTRN=L+1
      NC=NC+1
      GO TO 40
153  RATIO=(TL-OT(1))/OT(1)*1.0+0.9*RATIO
      NCASE=NCASE+(OT(1)-OT(1))-OT(1)
      OT(1)=OT(1)+RATIO
      NC=NC+1
      GO TO 40
155  PRINT 3323
153  FORMAT(1H0,1HTEMPERATURE,1X,7HPROFILE,1X,7HDEFINED)
      CALCULATION OF PRESSURE PROFILE
      OT(1)=TL-T(1))
      SIMP1=0.0
      SIMP2=0.0
      SIMP3=0.0
      SIMP4=0.0
      LS=ZL/25
      JS=(1.0-0.9*ZL+5.0)/10.0
      LS=JS+1
      ZX(LS)=ZL
      T2(LS)=TL
      P(LS)=PL
      U(1)=260.0,J=1,JS
      MBAR=M-1
      MBAR=MBAR
      LS=LS-MBAR
      LS=LS-MBAR
      ZY(1)=ZX(LS)-MBAR
      ZSIMP=JS/ZSIMPI
      JS=(1.0-0.9*ZSIMP+5.0)/10.0
      JS=JS+1
      ZY(1)=ZY(1)-MBAR
      U(J)=U(J)-MBAR
      MBAR=MBAR
      MBAR=MBAR
      ZY(1)=ZY(1)-MBAR
      ZSIMP=JS/ZSIMPI

```

## FORTRAN SOURCE LIST TEPRE

## SOURCE STATEMENT

```

ZVIR=ZY(10)
100 I=1,NC
CALL OMCA(TVAR,Z,T,ITEMP,NDIM2,TVIS)
205 TK=(TVIS+450.)/1.8
209 DO 210 I=1,NC
213 TK=(1.8/CF(I))*TK
214 IMAX=IPDATA
215 CALL OMCA(TKE,KTE,ZOMGA,IMAX,NDIM3,Onga)
216 VIS(I)=2.6693*10.**(-3.)*(FW(I)*TK)**0.5/(SIG(I)**2.0)*Onga
217 CONTINUE
218 IF(NC-1)238,238,220
220 GO TO(222,221,221),KEY
221 TVAR=TK
222 DO217 KL=2,AN4
223 CALL OMCA(TVAR,TABLE(1,1),TABLE(1,KL),KMAX,NDIM1,
1 VARY)
224 IF(KL.GT.2)GO TO 214
225 REACT=VARY
226 GO TO 217
227 IF(KL.GT.3)GO TO 215
228 AVGFW=VARY
229 GO TO 217
230 IF(KL.GT.4)GO TO 219
231 W=VARY
232 GO TO 217
233 Y(KL-4)=VARY
234 IF(Y(KL-4))216,216,217
235 Y(KL-4)=1.0E-10
236 CONTINUE
237 V/TK=0.0
238 DO 239 J=1,NC
239 TTERM=1.0
240 DO 241 L=1,NC
241 TTV=L/226,225,226
242 DO 243 L=1,NC
243 TTVY=(1.0+(VIS(J)/VIS(L))**0.5*(FW(L)/FW(J))**0.25)**2.0
244 SCTV=2.0*SQT(2.0)*(1.+FW(J)/FW(L))**0.5
245 PHTV=TTVY/SCTV
246 TTERM=TTERM+PTTV*(Y(L)/Y(J))
247 CONTINUE
248 PHTV=Y(J)*(VIS(J)/TTERM)
249 CONTINUE
250 GO TO 2380
251 VISG=VIS(I)*2.42/3600.0
252 GO TO 253
253 VISGDS=VIS(I)*2.42/3600.0
254 TT(-1)=(TVIS/AVGFW)**0.5
255 PREC(1,1)=TVIS*VISGDS/AVGFW
256 CALL OMCA(TVIS,T,CAPAC,ITEMP,NDIM2,CPBAR)
257 PREC(1,1)=CPBAR*W
258 GO TO(240,2391,2491),KEY
259 PRDOR(1,1)=REACT
260 CONTINUE
261 ZX(LD-1)=ZX(LD)+HS
262 TP(LD-1)=TT(1)*AVGFW/0.5

```

## FORTRAN SOURCE LIST FEMPRE

## SOURCE STATEMENT

```

251 T=TP(L0)-TP(L0-1)
252 SUM1=0.0
253 SUM2=0.0
254 SUM3=0.0
255 SUM4=0.0
256 SUM5=0.0
257 SUM6=0.0
258 SUM7=0.0
259 SUM8=0.0
260 MEVEN=ME-1
261 DO255 KP=2,MEVEN,2
262 SUM1=SUM1+4.0*PRGD0(KP)
263 SUM3=SUM3+4.0*TT(KP)
264 SUM5=SUM5+4.0*PRODCP(KP)
265 GO TO(255,2640,2540),KEY
266 SUM7=SUM17+4.0*PRODR(KP)
267 CONTINUE
268 NOLP=1P-2
269 DO256 KP=3,NODC,2
270 SUM2=SUM2+2.0*PROD(KP)
271 SUM4=SUM4+2.0*TT(KP)
272 SUM6=SUM6+2.0*PRODCP(KP)
273 GO TO(256,2570,2570),KEY
274 SUM8=SUM8+2.0*PRODR(KP)
275 CONTINUE
276 SIMPL=(HSI*PI/3.0)*(PRGD(1)+PRGD(MP)+SUM1+SUM2)+SIMP1
277 SIMP2=(HSI*PI/3.0)*(TT(1)+TT(MP)+SUM3+SUM4)+SIMP2
278 P(L0+1)=SQRT(PL*32+(2.*RR)*(773.16/32.0)*(ALPHA*SIMP1+BETA*SIMP2))
279 SIMP3=DELTA*HSIMPL/(HS*3.0)*(PRDCP(1)+PRODCP(KP)+SUM5+SUM6)+SIMP3
280 GO TO(260,258,258),KEY
281 SIMP4=DELTA*HSIMPL/(HS*3.0)*(PRCDR(1)+PRODR(MP)+SUM7+SUM8)+SIMP4
282 CONTINUE
283 GO TO(2600,2601,2601),KEY
2840 CL=EPS+SIMP3
2850 GO TO 261
2860 CL=EPS*(SIMP3+SIMP4)
2870 PRINT 262
2880 FORMAT(1H0,SH(I),3X,SHZX(I),10X,SHTP(I),11X,4HP(I))
2890 DO163 I=1,LS
2900 PRINT266,I,ZX(I),TP(I),P(I)
2910 FORMAT(1H0,15,3E15.6)
2920 CONTINUE
2930 PRINT2630
2940 FORMAT(1H0,36HTEMPERATURE-PRESSURE PROFILES DEFINED.,10X,21HHEAT F
2950 ULUX CALCULATED.)
2960 QCL=(P(1)-PL)
2970 GO TO(270,2751,2753),KEY
2980 PRINT2700
2990 FORMAT(1H0,20X,14HFROZEN FLOW RESULTS)
3000 GO TO 271
3010 PRINT2702
3020 FORMAT(1H0,21X,24HEQUILIBRIUM FLOW RESULTS)
3030 GO TO 271
3040 PRINT2704

```

## FORTRAN SOURCE LIST TEPRE

SOURCE STATEMENT

```

      C(F(1))=F(1)
      SF=10,138
      L1 FC=F(1)
      TPREV=T(1+1)

      T1=TA=F(1)
      L2 DTC=D(T(1))
      C(TA)=AT(M)
      MX=1
      ZT(1)=T(1)+1000,1100,103
      L16 UT(1)=SI(1)/(1.0E0,5*((TL-TCHECK)/TL))*2.0
      GO TO 40
      L3 APK=.5*ESTC
      886 RMSEI=FC+660.0
      FVAR=RAKEM/1.8
      NOW=TC
      DEL=NOW-TPREV
      DELZ=DEL/DTC

      SC TO (58,60,61),KEY
      58 AVGFM=0.0
      DO 59 I=1,NC
      AVGFM=AVGFM+(F(I)*FW(I))
      59 CONTINUE
      GO TO 104
      60 IF(KOUNT,80,2)GO TO 710
      CALL KOLERA(KOUNT,KP13,TABLE,K6)
      KOUNT=2
      KMAX=KP13
      DO 707 KL=2,KMAX
      CALL CRGCA(TVAR,TABLE(1,1),TABLE(1,KL),KMAX,NDDM1,
      VARY)
      IF(LL,GT,2)GO TO 704
      REACT=VARY
      GO TO 707
      704 IF(KL,GT,3)GO TO 705
      AVGFM=VARY
      GO TO 707
      705 IF(KL,GT,4)GO TO 708
      d=VARY
      GO TO 707
      708 Y(KL-4)=VARY
      IF(Y(KL-4))706,706,707
      706 Y(KL-4)=1.0E-10
      707 CONTINUE
      708 CALL KLAFT(TP1,TVAR,DELTZ,KN,K7,
      DTC,REACT,M,KPTD,TABLE,AVGFM)
      KN=2
      KMAX=KP13
      K7=2
      704 CALL FCPFT(TVAR,UNCHAR,NDATA,XTRK,ZDPA,NDDM1,CPRX,CD0,DC00)
      704 UNCHAR=(1.0*XAVGFM)*RR
      704 T=1.0*(T(1)-TC)+2.0*(1054+106,106,107)
      704 UNCHAR=Y(1)*T*FC
      704 Y(1)=Y(1)+0.2*FC(Z)
      707 GO TO (58,60,61),KEY

```

## FORTRAN SOURCE LIST PRCPT

## SOURCE STATEMENT

```
50  CCCN=CDO  
DELTF=DELTK*1.8  
CCCC=(CCCP-CCDN)/(DELT*2.0)  
TC=T  
GO TO 500  
500 RETURN  
END
```

## FORTRAN SOURCE LIST TEMPRE

## SOURCE STATEMENT

```
2704      FORMAT(1H0,25X,28HNON-EQUILIBRIUM FLOW R
1RESULTS)
271 PRINT 272
272 FORMAT(1H0,3X,5FDELT,6X,4HDELP,7X,2HQL)
PRINT273,DELT,DELP,QL
273 FORMAT(1H0,3F10.4)
SWITCH NO. 1 = OFF, SWITCH NO. 2 = OFF --- GO TO NEW CASE
SWITCH NO. 1 = OFF, SWITCH NO. 2 = ON --- FROZEN TO NON-EQUILIBRIUM
SWITCH NO. 1 = ON, SWITCH NO. 2 (NOT NEEDED) --- JOBS IN SEQUENCE
CALL SSWTCH(1,JOB)
GO TO(274,275),JOB
274 KEY=KEY+1
IF(KEY=3)2740,2740,278
2740 GO TO 30
275 IF(KEY=1)276,276,278
276 CALL SSWTCH(2,JIB)
GO TO(277,278),JIB
277 KEY=KEY+2
IF(KEY=3)2770,2770,278
2770 GO TO 30
278 GO TO 10
300 STOP
END
```

## FORTRAN SOURCE LIST

## SOURCE STATEMENT

```

SIBFTC PROPT
C   SUBROUTINE PROPT (HEAT CAPACITY AND CONDUCTIVITY VS. TEMPERATURE)
C   SUBROUTINE PROPT(TVAR,JCHAR,NDATA,XTKE,ZOMGA,NDIM3,CPMX,CDO,DCDO)
C   DIMENSION ICODE(20),ALPA(20),AA(20,6),
C   1 S1(4),S2(4),S3(4),S4(4),S5(4),A11(4),A22(4),A33(4),A44(4),A55(4)
C   DIMENSION AI(20),BI(20),CI(20),DI(20),EI(20),FI(20),GI(20),
C   1 AII(20),BII(20),CII(20),DII(20),EII(20),FII(20),GII(20),FW(20),
C   2 YI(20),EK(20),SIG(20),Y(20)
C   DIMENSION CP(20),CV(20),COND(20),XTKE(100),ZOMGA(100)
C   COMMON NC,NS,MM,WI,PL,RR,TZERO,DELTK,ICODE,ALPA,AA,S1,S2,S3,
C   1 S4,S5,A11,A22,A33,A44,A55
C   COMMON AI,EI,CI,DI,EI,FI,GI,AII,BII,CII,DII,EII,FII,GII,FW,YI
C   COMMON EK,SIG,EPS,Y
C   RANKIN=1.8*TVAR
C   FAREN=RANKIN-460.0
C   T=TVAR
C   TC=T+DELT K
500  DC516 I=1,NC
      TKE=(1.0/EK(I))*TC
      IMAX=N DATA
      CALL OMEGA(TKE,XTKE,ZOMGA,IMAX,NDIM3,OMGA)
      IF(TC-1000.0)505,505,506
505  CP(I)=AII(I)+BII(I)*TC+CI(I)*TC**2+DII(I)*TC**3+EII(I)*TC**4
      GO TO 507
506  CP(I)=AI(I)+BI(I)*TC+CI(I)*TC**2+DI(I)*TC**3+EII(I)*TC**4
507  CV(I)=(CP(I)-RR)
      TOP=2.693*10.0**(-5.0)*(TC/FW(I))**0.5*(CV(I)+4.47)
      BOT=(SIG(I)**2.0*OMGA)
      COND(I)=TOP/BOT
516  CONTINUE
      CPMX=0.0
      CDMX=0.0
      DC537 J=1,NC
      SUMCP=CP(J)*Y(J)
      CPMX=CPMX+SUMCP
      SUMCD=COND(J)*Y(J)
      CDMX=CDMX+SUMCD
537  CONTINUE
      GO TO (538,539),JCHAR
538  CALL CHAR(SLOPE,YINTCP,KODE)
539  SCHAR=SLOPE
      YCHAR=YINTCP
      CCCHAR=(SCHAR*TC)+YCHAR
      CHARK=(CCCHAR*30.48)/(252.0*1.8)
      GASK=(CDMX*30.48)/(252.0*1.8)
      GO TO (5400,5401),KODE
5400  CDC=CHARK
      GO TO 5402
5401  CDC=GASK*EPS + CHARK*(1.0-EPS)
5402  IF(ABS(T-TC)-.00001)560,560,540
540  IF(T-TC)541,550,550
541  CDCP=CDO
      TC=T-DELT K
      JCHAR=2
      GO TO 500

```

## FORTRAN SOURCE LIST

## SCOURSE STATEMENT

```

1BFTC CMEGA
SUBROUTINE OMEGA (VAR,X,F,IMAX,NAME,SOM)
DIMENSION X(NAME),F(NAME),XN(300),FN(300)
NPTS=3
607 XUP=1.E30
DC611 I=1,IMAX
T=VAR-X(I)
IF(T)608,609,609
608 T=-T
609 IF(T-XUP)610,611,611
610 IP=I
XUP=T
611 CONTINUE
IN=1
NPP=NPTS+1
DC613 I=1,NPP
FN(I)=F(IP)
XN(1)=X(IP)
IF(IN)612,612,613
612 IQ=IP-1
GO TO 615
613 IQ=IP+1
IF(IMAX-IQ)614,615,615
614 IP=IP-1
GO TO 618
615 IF(IQ)616,616,617
616 IP=IP+1
GO TO 618
617 IP=IQ
IN=-IN
618 CONTINUE
SOM=0.0
FACT=1.0
DC620 J=1,NPTS
SOM=SOM+FACT*FN(1)
DC619 I=J,NPTS
IQ=I-J+1
619 FN(IQ)=(FN(IQ+1)-FN(IQ))/(XN(I+1)-XN(IQ))
620 FACT=FACT*(VAR-XN(J))
RETURN
END

```

## FORTRAN SOURCE LIST

## SOURCE STATEMENT

BFTC CHAR

SUBROUTINE CHAR (CHAR CONDUCTIVITY VS. TEMPERATURE---SLOPE AND INTERCEPT)

SUBROUTINE CHAR(SLOPE,YINTCP,KODE)

DIMENSION XCOND(100),YCOND(100)

MDATA=NO. OF XCOND VS. YCOND DATA POINTS

KODE= 1 (DATA WITH INERTS IN PORES) = 2 (DATA WITH EVACUATED PORES)

READ700,MDATA,KODE

XCOND=TEMPERATURE (OK)

YCOND=CHAR CONDUCTIVITY TABULATED VS TEMPERATURE (CAL/CM-SEC-OK)

READ701,(XCOND(I),YCOND(I),I=1,MDATA)

700 FORMAT(2I6)

701 FORMAT(F15.0,E15.5)

SUMX=0.0

SUMY=0.0

SUMXY=0.0

SUMX2=0.0

SUMY2=0.0

TN=MDATA

CC710 J=1,MDATA

SUMX=SUMX+XCOND(J)

SUMY=SUMY+YCOND(J)

SUMXY=SUMXY+XCOND(J)\*YCOND(J)

SUMX2=SUMX2+XCOND(J)\*\*2.0

SUMY2=SUMY2+YCOND(J)\*\*2.0

10 CONTINUE

20 SLOPE=(SUMXY-(SUMX\*SUMY/TN))/(SUMX2-(SUMX\*\*2.0/TN))

30 YINTCP=(SUMY-(SLOPE\*SUMX))/TN

RETURN

END

## FORTRAN SOURCE LIST

## SOURCE STATEMENT

IBFTC MCLFRA

SUBROUTINE MCLFRA(KOUNT,KPT3,TABLE,K6)

EDUARDO C. DEL VALLE-NASA PROJECT-135-30-8621-LSU PROJECT NO-04-1303-40068

CHEMICAL EQUILIBRIUM IN COMPLEX MIXTURE-METHOD OF WHITE-JOHNSON-DANTZIG

RAND METHOD(STEEPEST DESCENT), JOURNAL-CHEMICAL PHYSICS-VOL-28-N05-1958

DIMENSION ICODE(20),ALPA(20),AA(20,6),

1 S1(4),S2(4),S3(4),S4(4),S5(4),A11(4),A22(4),A33(4),A44(4),A55(4)

DIMENSION AI(20),BI(20),CI(20),DI(20),EI(20),FI(20),GI(20),

1 AII(20),EII(20),CII(20),DII(20),EIII(20),FII(20),GII(20),FW(20),

2 YI(20),EK(20),SIG(20),Y(20)

DIMENSION YAVG(20),XMW(20),YAVG1(20),X(20),FY(20),C(20),FORT(20),

1 F(31,31),B(31,1),PI(31),IPIVOT(30),BB(20),INDEX(31,2),BBP(31),

2 FSUM(20),YSUM(20),YY(20),XY(20),XMASS(20),YX(20),PERC(20),

3 DELTA(20),APART(20),BPART(20),ENT(20),DOTA(25,25),DOTA1(25,25),

4 CPDT(20),CPDT1(20),TABLE(30,30)

DIMENSION FD(4),DELH(5),FOHO(5)

COMMON NC,NS,MM,WI,PL,RR,TZERO,DELTk,ICODE,ALPA,AA,S1,S2,S3,

1 S4,S5,A11,A22,A33,A44,A55

COMMON AI,PI,CI,DI,EI,FI,GI,AII,BII,CII,DII,EIII,FII,GII,FW,YI

COMMON EK,SIG,EPS,Y

IF(K6.GT.1)GOTO3174

XT=INITIAL TEMPERATURE AT WHICH EQUILIBRIUM PROGRAM IS STARTED

TMAX=FINAL TEMPERATURE AT WHICH EQUILIBRIUM PROGRAM IS ENDED

TINC=TEMPERATURE INTERVAL IN EQUILIBRIUM PROGRAM CALCULATIONS

CRIT=CRITERION FOR CONVERGENCE IN EQUILIBRIUM PROGRAM

READ7,XT,TMAX,TINC,CRIT

NMAX=MAXIMUM SIZE OF THE SQUARE MATRIX

NFFEC=NO. AFTER WHICH TRACE COMPONENTS ARE CHECKED

READ2,NMAX,NFREQ

7 FORMAT(4E10.4)

2 FORMAT(2I6)

3174 K6=2

CALL FPTRAP(-3)

DO 3 I=1,NS

Y(I)=YI(I)

XMW(I)=FW(I)

3 CONTINUE

W=WI

NN=NC

NQ=NS

MA=1

NA=MM+1+NQ-NN

P=PL/2160.0

KPT=0

KPT1=0

MAXNT=100

KCCCE=0

KREAD=0

T=XT

KOS=NN+4

LL=NN+1

M=MA

N=NA

## FORTRAN SOURCE LIST MOLFRA

## SCOURCE STATEMENT

```

KX=0
XBETA=CRIT
500 PRINT4
4 FORMAT(//,6X,1H1,19X,5HF0/RT,13X,12HINITIAL Y(I)//)
DO 433 I=1,NQ
IF(ICODE(I).EQ.C)GOT0433
KCCDE=1
433 CONTINUE
45 NTEST=NFRER
NT=1

```

DELH(3) AND DELH(6) ARE THE HEATS OF FORMATION OF ETHANE AND BENZENE AT OK. RESPECTIVELY.

DELH(6)=2.4000E4  
DELH(3)=-1.6517E4

HC IS THE CHEMICAL POTENTIAL OF THE ELEMENTS, THAT IS, THE SENSIBLE ENTHALPY CHANGE FROM 298.15 DEGREES KELVIN TO OK., DIVIDED BY RR\*T.  
HC(1) AND HC(2) ARE THE SUBSCRIPT FOR CARBON AND HYDROGEN RESPECTIVELY.

HC(1)=-251.2/(RR\*T)  
HC(2)=-2023.8/(RR\*T)

```

IF(T.GT.1500.)GOT06205
50 41 I=1,NQ
APART(I)=AI(I)*(1.-ALOG(T))-BI(I)*T/2.-CII(I)*(T**2)/6.
BPART(I)=-DI(I)*(T**3)/12.-EI(I)*(T**4)/20.+FI(I)/T-GII(I)
FORT(I)=APART(I)+BPART(I)
PRINT14,ALPA(I),FORT(I),Y(I)
41 CONTINUE
4 FORMAT(1X,16,2E20.8)
GOT01020
205 DC 6206 I=1,NQ
APART(I)=AI(I)*(1.-ALOG(T))-BI(I)*T/2.0-CI(I)*(T**2)/6.0
BPART(I)=-DI(I)*(T**3)/12.0-EI(I)*(T**4)/20.0+FI(I)/T-GI(I)
FORT(I)=APART(I)+BPART(I)
PRINT14,ALPA(I),FORT(I),Y(I)
206 CONTINUE
320 IF(T.GT.1500.)GOT09131

```

F0HC(3) AND F0HC(6) REPRESENTS THE TERM F-H/(R\*T), WHICH IS CALCULATED USING THE DATA BY DUFF. (LOS ALAMOS SCIENTIFIC LABORATORY REPORT NUMBER 2556, SEPT 18, 1961), AND IT IS FOR ETHANE AND BENZENE RESPECTIVELY.

```

FORT(3)=FORT(3)+DELH(3)/(RR*T)+AA(3,1)*HO(1)+(AA(3,2)/2.)*HO(2)
FORT(6)=FORT(6)+DELH(6)/(RR*T)+AA(6,1)*HO(1)+(AA(6,2)/2.)*HO(2)
GO TO 1020
131 FORT(3)=FORT(3)+DELH(3)/(RR*T)+AA(3,1)*HO(1)+(AA(3,2)/2.)*HO(2)
FORT(6)=FORT(6)+DELH(6)/(RR*T)+AA(6,1)*HO(1)+(AA(6,2)/2.)*HO(2)
500 DO320J=1,MM
BB(J)=0.0

```

## FORTRAN SOURCE LIST MOLFRA

## SOURCE STATEMENT

```

DO 320 I=1,NQ
BB(J)=B3(J)+AA(I,J)*Y(I)
320 CONTINUE
300 YBAR=0.0
DC50I=1,NN
50 YBAR=YBAR+Y(I)
DC10I=1,NN
C(I)=FORT(I)+ALOG(P)
FAC=Y(I)/YBAR
IF(FAC.LT.1.E-38)FAC=1.E-38
FY(I)=Y(I)*(C(I)+ALOG(FAC))
10 CONTINUE
IF(KCODE.EQ.0)GOTO111
DC 11 I=LL,NQ
FY(I)=Y(I)*FORT(I)
11 CONTINUE
111 DC3CJ=1,MM
DC3CK=1,MM
ASUM=0.0
DC20I=1,NN
WAY=AA(I,J)*AA(I,K)*Y(I)
20 ASUM=ASUM+WAY
R(J,K)=ASUM
30 CONTINUE
DC70K=1,MA
DC70J=1,MM
SUM=0.
DC130I=1,NN
130 SUM=SUM+AA(I,J)*FY(I)
BSUM=SUM+BE(J)
B(J,K)=BSUM
70 CONTINUE
CSUM=0.0
DC80I=1,NN
80 CSUM=CSUM+FY(I)
JJ=MM+1
DC91J=1,M
91 B(JJ,J)=CSUM
DC 103 K=1,MM
CSUM=0.0
DC 101 I=1,NN
101 DSUM=DSUM+AA(I,K)*Y(I)
BBP(K)=DSUM
103 CONTINUE
DC90J=1,MM
90 R(J,JJ)=BBP(J)
DC94K=1,MM
94 R(JJ,K)=R(K,JJ)
KK=MM+1
KL=JJ
IF(KCODE.EQ.0)GOTO1050
DO 29 I=LL,NQ
KK=KK+1
DC 29 J=1,MM
R(J,KK)=AA(I,J)

```

## FORTRAN SOURCE LIST MOLFRA

## SOURCE STATEMENT

```

25 CONTINUE
  KL=NQ-NN+JJ
  KK=MM+2
  DO 95 K=KK,KL
  DO 97 J=1,MM
  97 R(K,J)=R(J,K)
  95 CONTINUE
  KM=MM+1
  DO 1052 J=1,MA
  DO 1053 I=LL,NQ
  KM=KM+1
1053 B(KM,J)=FORT(I)
1052 CONTINUE
1050 CONTINUE
  DO 1044 J=JJ,KL
  DO 1045 K=JJ,KL
1045 R(J,K)=0.0
1044 CONTINUE
  24 FORMAT(E16.8)
  CALL MATINV(R,N,B,M,DETERM,IPIVOT,INDEX,NMAX,ISCALE)
  DO1001=1,JJ
1001 PI(I)=B(I,M)
  U=PI(JJ)
  XBAR=U*YBAR
  IF(KCODE.EQ.0)GOTO59
  KK=MM+2
  LW=LL
  DO 1002 J=KK,KL
  X(LW)=B(J,M)
1002 LW=LW+1
  55 DO60I=1,NN
  60 FSUM(I)=-FY(I)+(Y(I)/YBAR)*XBAR
  DO110I=1,NN
  PSUM=0.
  DO120J=1,MM
120  PSUM=PSUM+PI(J)*AA(I,J)
  YSUM(I)=PSUM*Y(I)
  110 X(I)=FSUM(I)+YSUM(I)
  XLAMBD=1.
  310 DO 86 I=1,NQ
  DELTA(I)=X(I)-Y(I)
  86 CONTINUE
  DEBAR=0.
  DO87I=1,NN
  87 DEBAR=DEBAR+DELTA(I)
  93 DFDL=0.
  DO88I=1,NQ
  IF(ICODE(I).EQ.1)GOTO83
  96 FAC=(Y(I)+XLAMBD*DELTA(I))/(YBAR+XLAMBD*DEBAR)
  98 IF(FAC.GT.5.)GOTO82
  99 XLAMBD=.9*XLAMBD
  IF(XLAMBD.GT.1.0E-20)GOTO96
  82 DFDL=DFDL+DELTA(I)*(C(I)+ALOG(FAC))
  GOTO88
  83 DFDL=DFDL+DELTA(I)*FORT(I)

```

## FORTRAN SOURCE LIST MOLFRA

## SOURCE STATEMENT

```

88 CONTINUE
IF(CFDI.LT.0.)GOTO89
XLAMBD=.9*XLAMBD
IF(XLAMBD.GT.1.0E-9)GOTO93
89 DO76I=1,NQ
Y(I)=Y(I)+XLAMBD*DELTAT(I)
76 CONTINUE
SUMY=0.
DO370I=1,NN
370 SUMY=SUMY+Y(I)
DO340I=1,NQ
340 PERC(I)=(Y(I)/SUMY)*100.
350 BETA=0.
DO85I=1,NQ
85 BETA=BETA+ABS(DELTAT(I))
IF(BETA.LT.XBETA)GOTO800
IF(KX.GT.0)GOTO560
560 IF(NT.GE.MAXNT)GOTO0600
NT=NT+1
IF(KX.GT.0)GOTO300
GOTO1000
600 XBETA=XBET+.000001
MAXNT=MAXNT+100
NT=NT+1
GOTO300
300 NN=NC
KX=KX+1
IF(KX.LT.2)GOTO300
201 PRINT16,NT
16 FORMAT(//1X,30HNT = NO. ITERATIONS REQUIRED = 15//)
PRINT201,XBETA
201 FORMAT(//1X,7HBETA = E12.4//)
PRINT204,P,T
PRINT32
204 FORMAT(////1X, 9HPRESSURE=E13.5,5X,6HTEMP =E13.5//)
32 FORMAT(//6X,1HI,21X,4HY(I),14X,7HPERCENT)
XSUMY=0.
DO530I=1,NN
XSUMY=XSUMY+Y(I)
580 CONTINUE
XMWGAS=0.0
DO81I=1,NN
XMWGAS=XMWGAS+XMW(I)*Y(I)
81 CONTINUE
DO 191I=1,NQ
XMASS(I)=Y(I)*XMW(I)/XMWGAS
191 CONTINUE
DO44I=1,NQ
44 PRINT19,I,ALPA(I),Y(I),PERC(I),XMASS(I)
1S FORMAT(1X,I6,3X,A6,3E20.8)
ENTGAS=0.
PRINT12
12 FORMAT(//1X,11HENTHALPY(I)//)
DO 78I=1,NQ
ENT(I)=(AII(I)+BII(I)*TZERO/2.+CII(I)*(TZERO**2)/3.+DII(I)*(TZERO*

```

## FORTRAN SOURCE LIST MOLFRA

## SOURCE STATEMENT

```

1*3)/4.+EII(I)*(TZERO**4)/5.+FII(I)/TZERO)*RR*TZERO
ENT(3)=-20.236E3
ENT(6)=19.820E3
IF(T.LT.1000.0)GOTO6207
CPDT(I)=(AI(I)*(T-TZERO)+BI(I)*(T**2-TZERO**2)/2.+CI(I)*(T**3-TZER
10**3)/3.+DI(I)*(T**4-TZERO**4)/4.+EI(I)*(T**5-TZERO**5)/5.)*RR
DO 296J=2,MM
CPDT1(J)=(S1(J)*(T-TZERO)+S2(J)*(T**2-TZERO**2)/2.+S3(J)*(T**3-TZE
1R0**3)/3.+S4(J)*(T**4-TZERO**4)/4.+S5(J)*(T**5-TZERO**5)/5.)*RR*.5
96 CONTINUE
CPDT1(1)=(S1(1)*(T-TZERO)+S2(1)*(T**2-TZERO**2)/2.+S3(1)*(T**3-TZE
1R0**3)/3.+S4(1)*(T**4-TZERO**4)/4.+S5(1)*(T**5-TZERO**5)/5.)*RR
PRINT6021,CPDT(I),ENT(I),T
GOTO6291
07 CPDT(I)=(AII(I)*(T-TZERO)+BII(I)*(T**2-TZERO**2)/2.+CII(I)*(T**3-
1TZERO**3)/2.+DII(I)*(T**4-TZERO**4)/4.+EII(I)*(T**5-TZERO**5)/5.)*
2RR
DO297J=2,MM
CPDT1(J)=(A11(J)*(T-TZERO)+A22(J)*(T**2-TZERO**2)/2.+A33(J)*(T**3-
1TZERO**3)/3.+A44(J)*(T**4-TZERO**4)/4.+A55(J)*(T**5-TZERO**5)/5.)*
2RR*.5
297 CONTINUE
CPDT1(1)=(A11(1)*(T-TZERO)+A22(1)*(T**2-TZERO**2)/2.+A33(1)*(T**3-
1TZERO**3)/3.+A44(1)*(T**4-TZERO**4)/4.+A55(1)*(T**5-TZERO**5)/5.)*
2RR
291 RSUM=0.
DO 398 J=1,MM
398 RSLM=RSUM+AA(I,J)*CPDT1(J)
PRINT6021,CPDT(I),ENT(I),T
021 FCRMAT(1H0,3E15.5)
ENT(I)=ENT(I)+CPDT(I)-RSUM
ENT(1)=0.
ENT(7)=0.
ENT(9)=0.
ENT(13)=0.
PRINT6022,ENT(I),T
022 FCRMAT(1H0,2E15.5)
78 CONTINUE
ENTGAS=0.0
DO 781 I=1,NN
781 ENTGAS=ENTGAS+ENT(I)*Y(I)
DO79I=1,NQ
79 PRINT 24,ENT(I)
PRINT18,ENTGAS
18 FCRMAT(//1X,21HENTHALPY OF GAS MIX = E16.8)
XMWGAS=XMWGAS/XSUMY
PRINT17,XMWGAS
17 FCRMAT(//1X,28HMOLECULAR WEIGHT OF GAS MIX=E16.8//)
XPETA=CRIT
KPT=KPT+1
PRINT1112,W,T
112 FORMAT(1X,2E20.8)
IF(T.LT.998.)GOTO171
IF(KPT1.GT.0)GOTO171
KPT1=KPT

```

## FORTRAN SOURCE LIST MOLFRA

## SCURCE STATEMENT

```
171 TABLE(1,KPT)=T
      TABLE(3,KPT)=XMWGAS
```

## RECIFINE MOLE BASIS

```
IF(T.NE.XT)GOTO823
SUM1=0.
DO 822 I=1,NN
Y(I)=(W/XMWGAS)*PERC(I)/100.
```

```
822 SUM1=SUM1+Y(I)
Y(INC)=PERC(NQ)*SUM1/100.
RIN=PERC(NQ)/100.*XMW(NQ)/XMWGAS
ROUT=RIN
GOTO1711
823 WG=W
RCUT=PERC(NQ)/100.*XMW(NQ)/XMWGAS
RATIO=(1.+RIN)/(1.+ROUT)
W=VG*RATIO
RIN=ROUT
1711 TABLE(4,KPT)=W
```

## CALCULATION OF INDIVIDUAL MASS FLUXES

```
DO 1712 I=1,NN
FLUX=W/XMWGAS*PERC(I)/100.*XMW(I)
1712 DOTA(I,KPT)=FLUX
FLUX=W*ROUT
DCTA(NQ,KPT)=FLUX
DO 444 I=5,KOS
TABLE(I,KPT)=PERC(I-4)/100.
```

```
444 CONTINUE
IF(T.GE.TMAX)GOTO333
T=T+TINC
```

```
KX=0
GOTO500
```

```
333 TPT1=KPT1
KPT3=KPT-3
KCUNT=2
DO 338 J=5,KOS
SUMY1=0.
DO 337 I=1,KPT1
337 SUMY1=SUMY1+TABLE(J,I)
YAVG(J-4)=SUMY1/TPT1
338 CONTINUE
```

```
KPT2=KPT3-KPT1+1
TPT2=KPT2
```

```
DO 3338 I=5,KOS
SUMY1=0.
```

```
DO 3337 I=KPT1,KPT3
```

```
3337 SUMY1=SUMY1+TABLE(J,I)
YAVG1(J-4)=SUMY1/TPT2
3338 CONTINUE
```

```
DO 8000 J=1,KPT3
IF(J.GT.1)GOTO 732
```

```
DO 8001 I=1,NQ
```

## FORTRAN SOURCE LIST MOLFRA

## SOURCE STATEMENT

```

YPRIME=(1./(60.*TINC))*(-137.*DOTA(I,J)+300.*DOTA(I,J+1)-300.*DOTA
1(I,J+2)+200.*DCTA(I,J+3)-75.*DOTA(I,J+4)+12.*DOTA(I,J+5))
DCTA1(I,J)=YPRIME
8C01 CONTINUE
      GOTO 8004
732 IF(J.GT.2)GOTO733
      DO 8002 I=1,NQ
      YPRIME=(1./(60.*TINC))*(-12.*DOTA(I,J-1)-65.*DOTA(I,J)+120.*DOTA(I
1,J+1)-60.*DCTA(I,J+2)+20.*DOTA(I,J+3)-3.*DOTA(I,J+4))
      DCTA1(I,J)=YPRIME
8C02 CONTINUE
      GOTO 8004
733 DO 8C71 I=1,NQ
      YPRIME=(1./(60.*TINC))*(3.*DOTA(I,J-2)-30.*DOTA(I,J-1)-20.*DOTA(I,
1J)+60.*DOTA(I,J+1)-15.*DOTA(I,J+2)+2.*DOTA(I,J+3))
      DCTA1(I,J)=YPRIME
8C71 CONTINUE
8004 CONTINUE
8C05 CONTINUE
      SUM2=0.
      DO 8C07 J=1,KPT3
      DO 8C06 I=1,NQ
      SUM2=SUM2+DCTA1(I,J)*ENT(I)/XMW(I)
      TABLE(2,J)=SUM2
8C07 CONTINUE
      SUM=0.
      DO 200 J=1,KPT3
      200 SUM=SUM+TABLE(3,J)
      YFLCAT=KPT3
      YMWAvg=SUM/YFLCAT
      DO1I=1,30
      DO1J=1,I
      XXX=TABLE(I,J)
      TABLE(I,J)=TABLE(J,I)
      TABLE(J,I)=XXX
1      CONTINUE
      RETURN
      END

```

## FORTRAN SOURCE LIST

## SOURCE STATEMENT

1BFTC MATINV

MATRIX INVERSION WITH ACCOMPANYING SOLUTION OF LINEAR EQUATIONS  
 SUBROUTINE MATINV(A,N,B,M,DETERM,IPIVOT,INDEX,NMAX,ISCALE)

DIMENSION IPIVCT(N),A(NMAX,N),B(NMAX,M),INDEX(NMAX,2)  
 EQUIVALENCE (IROW,JROW), (ICOLUMN,JCOLUMN), (AMAX,T,SWAP)

## INITIALIZATION

```
5 ISCALE=0
6 R1=10.0**18
7 R2=1.0/R1
10 DETERM=1.0
15 DO 20 J=1,N
20 IPIVCT(J)=0
30 DO 550 I=1,N
```

## SEARCH FOR PIVOT ELEMENT

```
40 AMAX=0.0
45 DO 105 J=1,N
50 IF (IPIVCT(J)-1)60,105,60
60 DO 100 K=1,N
70 IF (IPIVOT(K)-1)80,100,740
80 IF (ABS(AMAX)-ABS(A(J,K)))85,100,100
85 IROW=J
90 ICOLUMN=K
95 AMAX=A(J,K)
100 CONTINUE
105 CONTINUE
110 IF (AMAX)110,1C6,11C
115 DETERM=0.0
120 ISCALE=0
125 GO TO 740
130 IPIVCT(ICOLUMN)=IPIVOT(ICOLUMN)+1
```

## INTERCHANGE ROWS TO PUT PIVOT ELEMENT ON DIAGONAL

```
130 IF (IROW-ICOLUMN)140,260,140
140 DETERM=-DETERM
150 DO 200 L=1,N
160 SWAP=A(IROW,L)
170 A(IROW,L)=A(ICOLUMN,L)
200 A(ICOLUMN,L)=SWAP
205 IF(M)260,260,210
210 DO 250 L=1,M
220 SWAP=B(IROW,L)
230 B(IROW,L)=B(ICOLUMN,L)
250 B(ICOLUMN,L)=SWAP
260 INDEX(I,1)=IROW
270 INDEX(I,2)=ICOLUMN
310 PIVCT=A(ICOLUMN,ICOLUMN)
```

## SCALE THE DETERMINANT

## FORTRAN SOURCE LIST MATINV

## SOURCE STATEMENT

```

100C PIVCTI=PIVOT
1005 IF(ABS(DETERM)-R1)1030,1010,1010
1010 DETERM=DETERM/R1
1011 ISCALE=ISCALE+1
1012 IF(ABS(DETERM)-R1)1060,1020,1020
1020 DETERM=DETERM/R1
1021 ISCALE=ISCALE+1
1022 GO TO 1060
1030 IF(ABS(DETERM)-R2)1040,1040,1060
1040 DETERM=DETERM*R1
1041 ISCALE=ISCALE-1
1042 IF(ABS(DETERM)-R2)1050,1050,1060
1050 DETERM=DETERM*R1
1051 ISCALE=ISCALE-1
1060 IF(ABS(PIVCTI)-R1)1090,1070,1070
1070 PIVCTI=PIVCTI/R1
1071 ISCALE=ISCALE+1
1072 IF(ABS(PIVCTI)-R1)320,1080,1080
1080 PIVCTI=PIVCTI/R1
1081 ISCALE=ISCALE+1
1082 GO TO 320
1090 IF(ABS(PIVCTI)-R2)2000,2000,320
2000 PIVCTI=PIVCTI*R1
2001 ISCALE=ISCALE-1
2002 IF(ABS(PIVCTI)-R2)2010,2010,320
2010 PIVCTI=PIVCTI*R1
2011 ISCALE=ISCALE-1
320 DETERM=DETERM*PIVOT

```

C C DIVIDE PIVOT ROW BY PIVOT ELEMENT

```

330 A(ICOLUMN,ICOLUMN)=1.0
340 DO 350 L=1,N
350 A(ICOLUMN,L)=A(ICOLUMN,L)/PIVOT
355 IF(M) 380,380,360
360 DO 370 L=1,M
370 B(ICOLUMN,L)=B(ICOLUMN,L)/PIVOT

```

C C REDUCE NON-PIVOT ROWS

```

380 DO 550 L1=1,N
390 IF(L1-ICOLUMN)400,550,400
400 T=A(L1,ICOLUMN)
420 A(L1,ICOLUMN)=0.0
430 DO 450 L=1,N
450 A(L1,L)=A(L1,L)-A(ICOLUMN,L)*T
455 IF(M) 550,550,460
460 DO 500 L=1,M
500 B(L1,L)=B(L1,L)-B(ICOLUMN,L)*T
550 CONTINUE

```

C C INTERCHANGE COLUMNS

```

600 DO 710 I=1,N
610 L=N+1-I

```

## FORTRAN SOURCE LIST MATINV

## SOURCE STATEMENT

```
62C IF(INDEX(L,1)-INDEX(L,2))630,710,630
63C JROW=INDEX(L,1)
64C JCOLUMN=INDEX(L,2)
65C DC 705 K=1,N
66C SWAP=A(K,JROW)
67C A(K,JROW)=A(K,JCOLUMN)
70C A(K,JCOLUMN)=SWAP
705 CCNTINUE
71C CONTINUE
74C RETURN
END
```

## FORTRAN SOURCE LIST

## SOURCE STATEMENT

SETC KINET

```

SUBROUTINE KINET(TP1, TVAR, DELZ, KN, K7, DTC, HEAT, WNEW, KPT3, TABLE,
1  AVGFW)
  DIMENSION ICODE(20), ALPA(20), AA(20,6),
1  S1(4), S2(4), S3(4), S4(4), S5(4), A11(4), A22(4), A33(4), A44(4), A55(4)
  DIMENSION AI(20), BI(20), CI(20), DI(20), EI(20), FI(20), GI(20),
1  AII(20), BII(20), CII(20), DII(20), EII(20), FII(20), GII(20), FW(20),
2  YI(20), EK(20), SIC(20), Y(20)
  DIMENSION RSC(20,20), PSC(20,20), REX(20,20), PEX(20,20), AF(20),
1 SF(20), AEF(20), AR(20), SR(20), AER(20), EQN(20), XFW(20), PERCE(20),
2 FLUXMO(20), FLUXMA(20), C(20), FK(20), RK(20), RATE(20), Y1(20)
  DIMENSION TABLE(30,30), YTEMP(20), ENT(20), CPDT(20), CPDT1(20)
  COMMON NC, NS, MM, WI, PL, RR, TZERO, DELTK, ICODE, ALPA, AA, S1, S2, S3,
1  S4, S5, A11, A22, A33, A44, A55
  COMMON AI, BI, CI, DI, EI, FI, GI, AII, BII, CII, DII, EII, FII, GII, FW, YI
  COMMON EK, SIG, EPS, Y
  CALL FPTRAP(-3)
  DO300 I=1, NS
    XFW(I)=FW(I)
300 CONTINUE
  KSP1=NS
  KSP=NC
  IF(KN.EQ.1)K1=0
  IF(K1.EQ.0)K2=0
  IF(K1.EQ.0)W=WI
  IF(K1.EQ.0)T1=533.33
  IF(K1.EQ.0)DIF=10.
  IF(K7.EQ.0)GOTO88
  IF(K1.NE.0)GOTO74
  DO128 I=1, KSP1
128 Y1(I)=YTEMP(I)
  W=V1
  IF(K7.GT.1)GOTO74
88  DO 97 I=1, 20
    DO 97 J=1, 20
      TABLE(I,J)=0.
97  CONTINUE
  CO 82 I=1, 15
  DO 83 J=1, 15
    RSC(I,J)=0.
    PSC(I,J)=0.
    REX(I,J)=0.
    PEX(I,J)=0.
83  CONTINUE
82  CONTINUE
  READ EQN 1 CH4 = H2 + 0.5C2H6
  READ21, (EQN(I), I=1, 12)
  READ THE STOCHIOMETRIC COEFICIENTS OF THE EQUATION
  READ 22, RSC(1,2), DUM1, DUM2, PSC(1,1), PSC(1,3), DUM3
  READ THE EXPONENTS OF THE RATE EQUATION
  READ 22, REX(1,2), DUM4, DUM5, PEX(1,1), PEX(1,3), DUM6
  READ THE COEFFICIENTS OF THE FORWARD AND REVERSE REACTION RATE CONS.
  UNITS OF AF AND AR ARE IN GM-MOLES, CUBIC-CM, AND SECONDS
  UNITS OF AEF AND AER ARE IN KCAL PER GM-MOLE
  READ23, AF(1), SF(1), AEF(1)

```

## FORTRAN SOURCE LIST KINET

## SOURCE STATEMENT

```

READ23,AR(1),SR(1),AER(1)
C READ EQN 2 C2H6 = H2 + C2H4
READ21,(EQN(I),I=1,12)
READ22,RSC(2,3),DUM7,DUM8,PSC(2,1),PSC(2,4),DUM9
READ22,REX(2,3),DU10,DU11,PEX(2,1),PEX(2,4),DU12
READ23,AF(2),SF(2),AEF(2)
READ23,AR(2),SR(2),AER(2)
23 FORMAT(E8.0,1X,2F6.0)
22 FORMAT(6F4.0)
21 FCRMAT(12A6)
C READ EQN 3 C2H4 = H2 + C2H2
READ21,(EQN(I),I=1,12)
READ22,RSC(3,4),DU13,DU14,PSC(3,1),PSC(3,5),DU15
READ22,REX(3,4),DU16,DU17,PEX(3,1),PEX(3,5),DU18
READ23,AF(3),SF(3),AEF(3)
READ23,AR(3),SR(3),AER(3)
C READ EQN 4 C2H2 = 2C + H2
READ21,(EQN(I),I=1,12)
READ22,RSC(4,5),DU19,DU20,PSC(4,13),PSC(4,1),DU21
READ22,REX(4,5),DU22,DU23,PEX(4,13),PEX(4,1),DU24
READ23,AF(4),SF(4),AEF(4)
READ23,AR(4),SR(4),AER(4)
C READ EQN 5 C6H6 = 3C2H2
READ21,(EQN(I),I=1,12)
READ22,RSC(5,6),DU25,DU26,PSC(5,5),DU27,DU28
READ22,REX(5,6),DU29,DU30,PEX(5,5),DU31,DU32
READ23,AF(5),SF(5),AEF(5)
READ23,AR(5),SR(5),AER(5)
C READ EQN 6 NH3 = 0.5N2 + 1.5H2
READ 21,(EQN(I),I=1,12)
READ22,RSC(6,8),DU33,DU34,PSC(6,7),PSC(6,1),DU35
READ22,REX(6,8),DU36,DU37,PEX(6,7),PEX(6,1),DU38
READ23,AF(6),SF(6),AEF(6)
READ23,AR(6),SR(6),AER(6)
C READ EQN 7 CH4 + 2O2 = CO2 + 2H2O
READ 21,(EQN(I),I=1,12)
READ22,RSC(7,2),RSC(7,9),DU39,PSC(7,10),PSC(7,12),DU41
READ22,REX(7,2),REX(7,9),DU42,PEX(7,10),PEX(7,12),DU43
READ23,AF(7),SF(7),AEF(7)
READ23,AR(7),SR(7),AER(7)
C READ EQUATION 8 C + H2O = CO + H2
READ 21,(EQN(I),I=1,12)
READ 22,RSC( 8,13),RSC( 8,12),PSC( 8,11),PSC( 8,1)
READ 22,REX( 8,13),REX( 8,12),PEX( 8,11),PEX( 8,1)
READ23,AF(8),SF(8),AEF(8)
READ23,AR(8),SR(8),AER(8)
C READ EQN 9 CH4= 0.5C2H2 + 1.5H2
READ 21,(EQN(I),I=1,12)
READ 22,RSC(9,2),PSC(9,5),PSC(9,1)
READ 22,REX(9,2),PEX(9,5),PEX(9,1)
READ23,AF(9),SF(9),AEF(9)
READ23,AR(9),SR(9),AER(9)
C READ EQN 10 CH4 = C + 2H2
READ 21,(EQN(I),I=1,12)
READ 22,RSC(10,2),PSC(10,13),PSC(10,1)

```

## FORTRAN SOURCE LIST KINET

## SOURCE STATEMENT

```

READ 22,PEX(10,2),PEX(10,13),PEX(10,1)
READ 23,AF(10),SF(10),AEF(10)
READ 23,AR(10),SR(10),AER(10)
C READ THE NUMBER OF SPECIES-KSP AND THE NUMBER OF EQUATIONS-NEQ
C READ THE MOLECULAR WEIGHTS OF THE SPECIES
READ24,NEQ
24 FORMAT(16)
C CONVERT TO KINET UNITS
  DC 127 I=1,KSP1
    Y1(I)=YI(I)
127 YTEMP(I)=Y1(I)
74 K1=K1+1
P=PL/2160.
R=82.06
RR=1.987
DELZ=DELZ*30.48
75 FORMAT(1X,I6)
IF(K1.GT.1)GOT03
C INITIAL AVERAGE MOLECULAR WEIGHT
C
PRINT 2137
2137 FORMAT(//2CX,4CHINITIAL MOLE FRACTION MOLECULAR WEIGHT//)
SUM=C.
DC1J=1,KSP
SUM=SUM+XFW(J)*Y1(J)
PRINT 250,Y1(I),XFW(I)
250 FORMAT(22X,1E17.8,5X,1E16.8)
1 CCNTINUE
PRINT 250,Y1(KSP1),XFW(KSP1)
AVCFW=SUM
C INITIAL MOLAL FLUX OF SPECIE J(GM-MOLES/CM2-SEC)
C
DC02J=1,KSP1
FLUXMO(J)=(W/AVGFW)*(454./923.03)*Y1(J)
C INITIAL MASS FLUX OF SPECIE J(GRAMS/CM2-SEC)
C
2 FLUXMA(J)=FLUXMO(J)*XFW(J)
C CALCULATION OF C(J)
C
IF(K1.GT.1)COT03
TZERO=298.16
T=(TP1 +460.)/1.8
GOT04
3 T=TVAR
4 SUM1=0.
IF(T.LT.T1)GOT073
K2=K2+1
KDS=KSP+4
DC17 I=5,KDS
TABLE(K2,I)=Y1(I-4)
17 CCNTINUE

```

## FORTRAN SOURCE LIST KINET

## SCURCE STATEMENT

```

73 DO5J=1,KSP
      SUM1=SUM1+FLUXMO(J)*R*T/P
      SUM=C.
      DO6J=1,KSP
      C(J)=FLUXMO(J)/SUM1
      E SUM=SUM+C(J)
      C(KSP1)=SUM*Y1(KSP1)

```

C  
C     CALCULATE REACTION RATE CONSTANT  
C

```

DC7I=1,NEQ
FK(I)=AF(I)*T**(-SF(I))*EXP(-AEF(I)*1000./(RR*T))
7 RK(I)=AR(I)*T**(-SR(I))*EXP(-AER(I)*1000./(RR*T))

```

C  
C     CALCULATION OF REACTION RATE OF SPECIE(J)  
C

```

DC12J=1,KSP1
SUM2=0.
DC11I=1,NEQ
XMULTR=1.0
XMULTP=1.0
DC10K=1,KSP1
IF(C(K).LT.1.E-37)C(K)=1.E-37
XMULTR=XMULTR*(C(K)**REX(I,K))
XMULTP=XMULTP*(C(K)**PEX(I,K))
10 CONTINUE
SUM2=SUM2+(PSC(I,J)-RSC(I,J))*(FK(I)*XMULTR-RK(I)*XMULTP)
11 CONTINUE
RATE(J)=SUM2
12 CONTINUE
733 WNEW=0.
SUM3=0.

```

```

DC13J=1,KSP1
FLUXMA(J)=FLUXMA(J)+RATE(J)*DELZ*XFW(J)
IF(FLUXMA(J).LE.1.E-37)FLUXMA(J)=1.E-37
FLUXMO(J)=FLUXMA(J)/XFW(J)
IF(J.EQ.KSP1)GOTO13
WNEW=WNEW+FLUXMA(J)*923.03/454.
SUM3=SUM3+FLUXMO(J)

```

```

13 CONTINUE
DC14J=1,KSP
Y1(J)=FLUXMO(J)/SUM3
14 PERCE(J)=Y1(J)*100.

```

C  
C     CALCUALTION OF THE RATIO OF THE MOLES OF THE  
C     SOLID SPECIE TO THE MOLES OF GASES.  
C     Y1(KSP1)=FLUXMO(KSP1)/SUM3C  
C     SUM7 IS THE ENTHALPY OF THE GAS MIXTURE WITH RESPECT TO  
C     THE ELEMENTS AT THEIR STANDARD STATE OF(P=1ATM T=298 OK)

```

SUM7=0.
SUM=0.
DC 78I=1,KSP1
ENT(I)=(AII(I)+BII(I)*TZERO/2.+CII(I)*(TZERO**2)/3.+DII(I)*(TZERO*

```

## FORTRAN SOURCE LIST KINET

## SOURCE STATEMENT

```

1*3)/4.+EII(I)*(TZERO**4)/5.+FII(I)/TZERO)*RR*TZERO
ENT(3)=-20.236E3
ENT(6)=19.820E3
IF(T.LT.1000.0)GOT06207
CPDT(I)=(AI(I)*(T-TZERO)+BI(I)*(T**2-TZERO**2)/2.+CI(I)*(T**3-TZE-
10**3)/3.+DI(I)*(T**4-TZERO**4)/4.+EI(I)*(T**5-TZERO**5)/5.)*RR
DO 296 J=2,MM
CPDT1(J)=(S1(J)*(T-TZERO)+S2(J)*(T**2-TZERO**2)/2.+S3(J)*(T**3-TZE-
1R0**3)/3.+S4(J)*(T**4-TZERO**4)/4.+S5(J)*(T**5-TZERO**5)/5.)*RR*.5
296 CONTINUE
CPDT1(1)=(S1(1)*(T-TZERO)+S2(1)*(T**2-TZERO**2)/2.+S3(1)*(T**3-TZE-
1R0**3)/3.+S4(1)*(T**4-TZERO**4)/4.+S5(1)*(T**5-TZERO**5)/5.)*RR
GOTC6291
6207 CPDT(I)=(AII(I)*(T-TZERO)+BII(I)*(T**2-TZERO**2)/2.+CII(I)*(T**3-
1TZER0**3)/3.+DII(I)*(T**4-TZERO**4)/4.+EII(I)*(T**5-TZERO**5)/5.)*
2RR
DO 297 J=2,MM
CPDT1(J)=(A11(J)*(T-TZERO)+A22(J)*(T**2-TZERO**2)/2.+A33(J)*(T**3-
1TZER0**3)/3.+A44(J)*(T**4-TZERO**4)/4.+A55(J)*(T**5-TZERO**5)/5.)*
2RR*.5
297 CONTINUE
CPDT1(1)=(A11(1)*(T-TZERO)+A22(1)*(T**2-TZERO**2)/2.+A33(1)*(T**3-
1TZER0**3)/3.+A44(1)*(T**4-TZERO**4)/4.+A55(1)*(T**5-TZERO**5)/5.)*
2RR
6291 RSUM=0.
DO 398 J=1,MM
C
C RSUM IS THE ENTHALPY OF THE ELEMENTS OF THE ITH SPECIE AT TEMPERA-
C TURE T(OK) WITH RESPECT TO THEIR STANDARD STATE(P=1ATM. T=298 OK).
C
398 RSUM=RSUM+AA(I,J)*CPDT1(J)
ENT(I)=ENT(I)+CPDT(I)-RSUM
ENT(1)=0.
ENT(7)=0.
ENT(9)=0.
ENT(13)=0.
SUM=SUM+RATE(I)*ENT(I)
IF(I.EQ.KSP1)GOT078
SUM7=SUM7+Y1(I)*(ENT(I)+RSUM)
78 CONTINUE
HEAT=(SUM/252.)*(30.48**3)/DTC
KPT3=K2
IF(T.LT.T1)GOT037
T1=T1+55.55555
PRINT 889
889 FORMAT(//7X,8HENTHALPY,5X,13HMOLE FRACTION,5X,7HRATE(I),8X,9HFLUXM
1A(I)//)
DO 777 I=1,KSP1
PRINT 808,ENT(I),Y1(I),RATE(I),FLUXMA(I)
808 FORMAT(1X,4E16.8)
777 CONTINUE
TABLE(K2,1)=T
TABLE(K2,2)=HEAT
TABLE(K2,3)=AVGFW
TABLE(K2,4)=WNEW

```

## FORTRAN SOURCE LIST KINET

## SOURCE STATEMENT

```
PRINT 6021
6021 FORMAT(//2X,15HTEMPERATURE(OK),6X,4HHEAT,10X,9HMASS FLUX,9X,5HAvgF
1W//)
PRINT 6022,T,HEAT,WNEW,AvgFW
6022 FORMAT(1X,4E16.8)
PRINT 6032,SUM7
6032 FORMAT(//1X,36HENTHALPY OF THE REACTING GAS SYSTEM=,1E16.8)
37 SUM=0.
DO 111 I=1,KSP
SUM=SUM+XFN(I)*Y1(I)
111 CONTINUE
AvgFW=SUM
2211 FORMAT(1X,5E14.8/)
112 CUNTINUE
DO6606 IK=1,NC
Y(IK)=Y1(IK)
6606 CONTINUE
RETURN
END
```

ENTHALPY	MOLE FRACTION	RATE(I)	FLUXMA(I)
----------	---------------	---------	-----------

0.	0.24832489E-01	0.10555829E-03	0.68863822E-04
-0.21835453E-05	0.55668452E-00	-0.46370102E-04	0.12350086E-01
-0.20236000E-05	0.35522686E-05	0.14726862E-06	0.14776376E-06
0.88905566E-04	0.15687441E-05	0.12023008E-06	0.60904729E-07
0.52654235E-05	0.82673532E-05	0.37910340E-06	0.29804423E-06
0.19820000E-05	0.98974118E-22	-0.12132990E-25	0.10704271E-22
0.	0.80113050E-01	0.93403076E-12	0.31102993E-02
-0.13468053E-05	0.16792077E-03	-0.18630615E-11	0.39581678E-05
0.	0.86118263E-27	0.14039841E-29	0.38210798E-28
-0.94685054E-05	0.15137768E-01	-0.70199203E-30	0.92353931E-03
-0.27834013E-05	0.12123620E-02	0.12609923E-04	0.47068593E-04
-0.59907508E-05	0.32183853E-00	-0.13609923E-04	0.80325124E-02
0.	0.15449203E-01	0.31456975E-04	0.25706634E-01

TEMPERATURE(CK)	HEAT	MASS FLUX	AVGFW
-----------------	------	-----------	-------

0.14223403E-04	0.96301310E-03	0.49885977E-01	0.17699366E-02
----------------	----------------	----------------	----------------

ENTHALPY OF THE REACTING GAS SYSTEM= -0.15908107E-05

ENTHALPY	MOLE FRACTION	RATE(I)	FLUXMA(I)
----------	---------------	---------	-----------

0.	0.28116063E-01	0.13815831E-03	0.78117756E-04
-0.21846780E-05	0.55415560E-00	-0.61585103E-04	0.12317341E-01
-0.20236000E-05	0.93663723E-05	0.29181405E-06	0.41119139E-06
0.84491919E-04	0.12417002E-04	0.81772020E-06	0.48299213E-06
0.52601212E-05	0.30056943E-04	0.13353276E-05	0.10856339E-05
0.19820000E-05	0.98291681E-22	-0.24485321E-25	0.10650662E-22
0.	0.79961125E-01	0.21523266E-11	0.31102993E-02
-0.13473978E-05	0.16760221E-03	-0.43006532E-11	0.39581653E-05
0.	0.89811119E-27	0.14243908E-29	0.39925038E-28
-0.94715405E-05	0.15109060E-01	-0.71219539E-30	0.92353931E-03
-0.27933526E-05	0.16393433E-02	0.17696421E-04	0.63766588E-04
-0.59961114E-05	0.32079889E-00	-0.17696421E-04	0.80217772E-02
0.	0.15430168E-01	0.38998958E-04	0.25722736E-01

TEMPERATURE(CK)	HEAT	MASS FLUX	AVGFW
-----------------	------	-----------	-------

0.14828133E-04	0.12524803E-02	0.49853334E-01	0.17655207E-02
----------------	----------------	----------------	----------------

ENTHALPY OF THE REACTING GAS SYSTEM= -0.14854536E-05

ENTHALPY	MOLE FRACTION	RATE(I)	FLUXMA(I)
----------	---------------	---------	-----------

0.	0.31277198E-01	0.17888312E-03	C.87061729E-04
-0.21847249E 05	0.55167712E 00	-0.82311834E-04	0.12284978E-01
-0.20236000E 05	0.17520340E-04	0.57663911E-06	0.73153223E-06
0.88195344E 04	0.47078513E-04	0.28509407E-05	0.18346373E-05
0.52556908E 05	0.77825992E-04	0.36980169E-05	0.28162257E-05
0.19820000E 05	0.97436288E-22	-0.42760104E-25	0.10577542E-22
0.	0.79813195E-01	0.41837895E-11	0.31102993E-02
-0.13473254E 05	0.16729201E-03	-0.83675789E-11	0.39581619E-05
0.	0.92569896E-27	0.14409323E-29	0.41227708E-28
-0.94741997E 05	0.15081109E-01	-0.72046615E-30	0.92353931E-03
-0.28020883E 05	0.20390736E-02	0.21794521E-04	0.79462159E-04
-0.60004282E 05	0.31980262E 00	-0.21794521E-04	0.80116867E-02
0.	0.15410323E 01	0.46266120E-04	0.25737267E-01

TEMPERATURE(CK)	HEAT	MASS FLUX	AVGFW
0.15350336E 04	0.16531647E-02	0.49824035E-01	0.17613353E 02

ENTHALPY OF THE REACTING GAS SYSTEM= -0.13926436E 05

ENTHALPY	MOLE FRACTION	RATE(I)	FLUXMA(I)
0.	0.36405757E-01	0.24917514E-03	0.10164915E-03
-0.21839388E 05	0.54751668E 00	-0.12079509E-03	0.12229847E-01
-0.20236000E 05	0.29178963E-04	0.12864041E-06	0.12220664E-05
0.87941956E 04	0.18658784E-03	0.95402441E-05	0.72975610E-05
0.52512535E 05	0.23728701E-03	0.10313216E-04	0.86129315E-05
0.19820000E 05	0.95738038E-22	-0.72269475E-25	0.10425162E-22
0.	0.79568372E-01	0.79195565E-11	0.31102993E-02
-0.13467270E 05	0.16677854E-03	-0.15839113E-10	0.39581546E-05
0.	0.95838440E-27	0.14570407E-29	0.42837084E-28
-0.94769882E 05	0.15034848E-01	-0.72852036E-30	0.92353931E-03
-0.28112356E 05	0.26314467E-02	0.26539105E-04	0.10286231E-03
-0.60045977E 05	0.31322298E 00	-0.26539105E-04	0.79966430E-02
0.	0.15375523E 01	0.54291780E-04	0.25758160E-01

TEMPERATURE(CK)	HEAT	MASS FLUX	AVGFW
0.15889111E 04	0.24392515E-02	0.49782484E-01	0.17539373E 02

ENTHALPY OF THE REACTING GAS SYSTEM= -0.12914062E 05

T(1)=	500.000000	CT(1)=	25252.399902		
T(L)	CT(L)	XAXIS(L)	YAXIS(L)	CAPAC(L)	
500.00000	25252.39990	0.00000	0.00000	0.56901	1
505.25250	25252.39990	0.01000	0.00263	0.56901	2
510.58553	26030.03564	0.02000	0.00529	0.57053	3
516.08235	26827.36865	0.03000	0.00804	0.57210	4

521.74709	27644.66919	0.04000	0.01087	0.57371	5
527.58393	28482.20044	0.05000	0.01379	0.57537	6
533.54710	29340.21729	0.06000	0.01680	0.57708	7
539.79089	30218.96582	0.07000	0.01990	0.57885	8
546.16963	31118.68311	0.08000	0.02308	0.58066	9
552.73772	32039.59668	0.09000	0.02637	0.58254	10
559.49958	32981.92383	0.10000	0.02975	0.58446	11
566.45969	33945.87061	0.11000	0.03323	0.58645	12
573.62257	34931.63281	0.12000	0.03681	0.58848	13
580.99277	35939.39404	0.13000	0.04050	0.59058	14
588.57489	36969.32568	0.14000	0.04429	0.59274	15
596.37355	38021.58691	0.15000	0.04819	0.59496	16
604.39342	39096.32373	0.16000	0.05220	0.59724	17
612.63918	40193.66846	0.17000	0.05632	0.59958	18
621.11555	41313.74022	0.18000	0.06056	0.60198	19
629.82727	42456.64355	0.19000	0.06491	0.60445	20
638.77910	43622.46875	0.20000	0.06939	0.60698	21
647.97581	44811.29102	0.21000	0.07399	0.60958	22
657.42219	46023.17090	0.22000	0.07871	0.61224	23
667.12304	47258.15332	0.23000	0.08356	0.61497	24
677.06318	48513.26758	0.24000	0.08854	0.61776	25
687.30740	49797.52686	0.25000	0.09365	0.62063	26
697.80054	51101.92871	0.26000	0.09890	0.62356	27
708.56741	52429.45459	0.27000	0.10428	0.62656	28
719.61279	53780.06885	0.28000	0.10981	0.62963	29
730.94151	55153.71924	0.29000	0.11547	0.63276	30
742.55833	56553.33739	0.30000	0.12128	0.63597	31
754.46803	57969.83887	0.31000	0.12723	0.63924	32
766.67535	59412.12061	0.32000	0.13334	0.64258	33
779.18504	60877.06396	0.33000	0.13959	0.64599	34
792.00177	62264.53271	0.34000	0.14600	0.64947	35
805.13023	63874.37451	0.35000	0.15257	0.65301	36
818.57504	65406.41943	0.36000	0.15929	0.65662	37
832.34081	66960.48145	0.37000	0.16617	0.66029	38
846.43211	68536.35742	0.38000	0.17322	0.66403	39
860.85343	70133.82910	0.39000	0.18043	0.66784	40
875.60925	71152.66113	0.40000	0.18780	0.67171	41
890.75399	73392.69254	0.41000	0.19535	0.67564	42
906.14201	75053.38672	0.42000	0.20307	0.67963	43
921.92762	76734.73145	0.43000	0.21096	0.68368	44
938.06506	78436.34180	0.44000	0.21903	0.68779	45
954.55851	80157.90723	0.45000	0.22728	0.69196	46
971.41209	81899.10449	0.46000	0.23571	0.69619	47
988.62986	83659.59363	0.47000	0.24431	0.70047	48
1006.21579	85433.04199	0.48000	0.25311	0.70480	49
1024.17378	87237.07813	0.49000	0.26209	0.70919	50
1042.50766	89053.34082	0.50000	0.27125	0.71363	51
1061.22119	90987.45703	0.51000	0.28061	0.71812	52
1080.31804	92739.04688	0.52000	0.29016	0.72267	53
1099.80180	94607.72656	0.53000	0.29990	0.72726	54
1119.67599	96493.11133	0.54000	0.30984	0.73190	55
1139.94405	98294.81738	0.55000	0.31997	0.73660	56
1160.60933	100312.46191	0.56000	0.33030	0.74134	57
1181.67509	102245.67090	0.57000	0.34084	0.74614	58
1203.14456	104194.07813	0.58000	0.35157	0.75099	59
1225.02084	106157.33105	0.59000	0.36251	0.75589	60
1247.30659	108135.09473	0.60000	0.37365	0.76085	61
1270.00600	110127.05566	0.61000	0.38500	0.76587	62
1293.12079	112132.92676	0.62000	0.39656	0.77096	63

1316.65422	114152.45313	0.63000	0.40833	0.77612	64
1340.60912	116185.39355	0.64000	0.42030	0.78134	65
1364.98819	118230.76650	0.65000	0.43249	0.78632	66
1389.79390	120287.65723	0.66000	0.44490	0.79133	67
1415.02861	122355.66406	0.67000	0.45751	0.79636	68
1440.69458	124434.39160	0.68000	0.47035	0.80142	69
1466.79431	126523.45215	0.69000	0.48340	0.80650	70
1493.32901	128622.46484	0.70000	0.49666	0.81160	71
1520.30161	130731.05566	0.71000	0.51015	0.81671	72
1547.71375	132848.85938	0.72000	0.52386	0.82184	73
1575.56732	134975.52148	0.73000	0.53778	0.82699	74
1603.86414	137110.69531	0.74000	0.55193	0.83214	75
1632.60593	139254.04492	0.75000	0.56630	0.83730	76
1661.79436	141405.24414	0.76000	0.58090	0.84247	77
1691.43102	143563.97852	0.77000	0.59572	0.84765	78
1721.51746	145729.94531	0.78000	0.61076	0.85282	79
1752.05515	147902.85156	0.79000	0.62603	0.85800	80
1783.04549	150082.41797	0.80000	0.64152	0.86318	81
1814.48985	152268.37891	0.81000	0.65724	0.86835	82
1846.38954	154460.48438	0.82000	0.67319	0.87351	83
1878.74580	156658.50000	0.83000	0.68937	0.87867	84
1911.55984	158862.21484	0.84000	0.70578	0.88381	85
1944.83284	161071.44336	0.85000	0.72242	0.88894	86
1978.56592	163286.03906	0.86000	0.73928	0.89406	87
2012.76018	165505.90234	0.87000	0.75638	0.89916	88
2047.41672	167731.00977	0.88000	0.77371	0.90425	89
2082.53662	169901.45117	0.89000	0.79127	0.90931	90
2118.12103	172197.48242	0.90000	0.80906	0.91435	91
2154.17117	174439.60742	0.91000	0.82709	0.91937	92
2190.68835	176688.70508	0.92000	0.84534	0.92436	93
2227.67419	178946.18555	0.93000	0.86384	0.92932	94
2265.13065	181214.22852	0.94000	0.88257	0.93426	95
2303.06024	183496.11133	0.95000	0.90153	0.93917	96
2341.46631	185795.69531	0.96000	0.92073	0.94405	97
2380.35345	188123.14258	0.97000	0.94018	0.94890	98
2419.72806	190485.91797	0.98000	0.95986	0.95372	99
2459.59921	192900.24219	0.99000	0.97980	0.95852	100
2499.97977	195388.35938	1.00000	0.99999	0.95852	101

## TEMPERATURE PROFILE DEFINED

(I)	ZX(I)	TP(I)	P(I)
1	0.000010	500.250668	2178.869598
2	0.006940	783.832504	2175.997925
3	0.013870	1406.974976	2170.710266
4	0.020800	2500.000000	2160.000000

TEMPERATURE-PRESSURE PROFILES DEFINED. HEAT FLUX CALCULATED.

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DELT T DELP GL

2000.0000 18.8696 63.8702

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